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### RICE UNIVERSITY

A CHROMATOGRAPHIC STUDY OF THE OXYGEN EXCHANGE
REACTION BETWEEN CARBON MONOXIDE AND CARBON
DIOXIDE OVER A Cu-ZnO CATALYST

by

WILLIAM DAVID SMITH

A THESIS SUBMITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF

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### ABSTRACT

A CHROMATOGRAPHIC STUDY OF THE OXYGEN EXCHANGE
REACTION BETWEEN CARBON MONOXIDE AND CARBON
DIOXIDE OVER A Cu-ZnO CATALYST

by

### William David Smith

Perturbation chromatography and, more specifically, the use of isotopic tracers have been applied successfully to the investigation of equilibrium and nonequilibrium chemisorption and surface reaction in a gas-solid system.

The theoretical treatment of the problem resulted in equations describing the movement of tracer samples down a packed column when adsorption and reaction processes were at equilibrium. In general, the assumption that these processes were near equilibrium was not valid. In order to describe the data over the entire range of flow rates, it was necessary to solve the continuity equations numerically.

The experimental system consisted of carbon monoxide and carbon dioxide, along with their carbon-14 isotopes, in the presence of a copper-zinc oxide catalyst at 400°F.

The catalyst, Girdler G-66B, is a commercial low temperature

water gas shift catalyst.

A five step adsorption-reaction mechanism was found to fit the data very well. Simpler mechanisms were attempted and found to be qualitatively unsatisfactory. The mechanism assumes two different types of adsorption for both carbon monoxide and carbon dioxide. In each case only one form of adsorption is directly involved in the exchange reaction. The mechanism is not specific regarding the nature of the oxygen exchange on the surface.

A brief investigation of the carbon dioxide - helium system showed that carbon dioxide adsorption on this catalyst follows a Freundlich isotherm at 400°F. The existence of dissociative carbon dioxide adsorption was neither proven nor disproven.

The absence of Langmuir behavior in both systems leads to the conclusion that the surface of this catalyst is extremely heterogeneous energetically.

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# TABLE OF NOMENCLATURE

# Capital Letters

A	Concentration of unoccupied type "A" surface
	sites, moles/mole flowing phase
$A_{B}$	Bypass peak area
$A_{\mathbf{C}}$	Column peak area
Az	Concentration of type "A" surface sites, moles/
	mole flowing phase
В	Concentration of unoccupied type "B" surface
	sites, moles/mole flowing phase
B <sub>z</sub>	Concentration of type "B" surface sites, moles/
	mole flowing phase
С	Concentration of unoccupied type "C" surface
	sites, moles/mole flowing phase
$C_s$	Chart speed for long column operation
$c_{s1}$	Chart speed for short column operation, column
	peak
C <sub>s2</sub>	Chart speed for short column operation, bypass
	peak
$C_z$	Concentration of type "C" surface sites, moles/
	mole flowing phase
	9.9.9

D	Flowing phase dispersion coefficient
F*	Rate of the isotopic exchange reaction
$^{\mathtt{F}}\mathtt{k}$	Rate of surface reaction "k"
G*	Retention product defined in equation (II-14)
K	Equilibrium constant for the exchange reaction
K †	Equilibrium function for the exchange reaction,
	defined in equation (II-29)
K <sub>&amp;</sub>	Equilibrium constant for step "2" in the mech-
	anism
K' <sub>4</sub>	Equilibrium function for the surface reaction in
	the mechanism, mole B type C0/mole B type ${\tt C0}_2$
$^{ extsf{L}}\mathbf{r}$	Chart length between bypass and main peaks
$^{ extsf{L}}$ rl	Chart length between main peak and injection
$L_{r2}$	Chart length between bypass peak and injection
N	Number of tanks used to model the column
P <sub>a</sub>	Barometric pressure
P <sub>c</sub>	Average column pressure
$^{P}_{\mathrm{H}_{2}0}$	Vapor pressure of water at room temperature
Pi	Column inlet pressure
Po	Column outlet pressure
Q	Carrier gas flow rate, column conditions
$Q_{m}$	Carrier gas flow rate measured by soap bubble
	meter
R	Gas constant in ideal gas law
$R_{i}$	Source term for component "i" in the flowing
	phase

 $R_i^!$  Source term for component "i" in the flowing phase,  $R_i^! = R_i/c$ 

 $\overline{R}_{\mathbf{i}}$  Source term for component "i" in the stationary phase

 ${\rm T_{c}}$  Column temperature

 ${\tt T}_{\tt r}$  Room temperature

 ${\bf V}_{\bf G}$  Column free volume

 $V_t$  Tank volume,  $V_t = V_G/N$ 

## Small Letters

a	Constant in Langmuir isotherm expressions
Ъ	Constant in Langmuir isotherm expressions
С	Total molar concentration of the flowing phase
$\mathtt{c_i}$	Molar concentration of component "i" in the
	flowing phase
d	Constant in Freundlich isotherm expression
f	Constant in Freundlich isotherm expression
$\mathtt{f}_\mathtt{B}$	Fraction of flow through bypass
j	Index used to identify each tank in column model
k	Rate constant for step "a" in the mechanism
k t	Rate constant for step "'\lambda", $k_{\ell} = k_{\ell}$ (A, B, or C)
m	Mass of catalyst in the column
n	Number of components in carrier gas
n <sub>i</sub>	Surface concentration of component "i", moles i/
	mole flowing phase

n; Surface concentration of component "i", moles i/g catalyst Surface concentration of component "i" on site "M", moles i/mole flowing phase Rate for step " $\ell$ " in the mechanism r t Time tp Peak residence time tr Carrier gas residence time  $\overline{\mathbf{u}}$ Flowing phase velocity vector Average velocity of flowing phase Characteristic velocity of mass perturbation  $v_{c}$ v\* Characteristic velocity of tracer Flowing phase mole fraction of component "i" y<sub>i</sub> Axial distance

# Greek Letters

β	Column conversion constant, $\frac{m}{V_G}$ c
μi	Adsorption equilibrium function for component
	"i", mole i on surface/mole i flowing phase
$\mu_{\mathbf{i}}^{!}$	Adsorption equilibrium function for component
	"i", μ' = μ <sub>i</sub> /β
Μ μi	Adsorption equilibrium function for component
	"i" on site "M"

 $_{\mu}^{M'}$  Adsorption equilibrium function for component "i" on site "M",  $_{\mu}^{M'}$  =  $_{\mu}^{M}/\beta$ 

Vik Stoichiometric coefficient for component "i"

for the kth surface reaction

τ Dimensionless time

## Subscripts

i Component "i"

k Reaction "k"

\$\text{Step "\lambda" in the mechanism}\$

M Adsorption site "M"

# Superscripts

s Steady state

\* Radioactive component

## I. INTRODUCTION AND LITERATURE REVIEW

## I.1 Introduction

In the past chemisorption of gases on catalytic surfaces has been studied most often in static systems. In the past decade, however, perturbation chromatography and the use of distinguishable molecular pulses (tracers) has emerged as a valuable new approach in chemisorption studies.

In this work, the theory and practice of perturbation chromatography and the use of radioactive tracers has been applied to the investigation of carbon monoxide and carbon dioxide adsorption on a copper-zinc oxide surface. The solid used was Girdler G-66B, a commercial low temperature water gas shift catalyst.

The purpose of this work was twofold. First, it was desired to extend the application of perturbation chromatography to the study of chemisorption in the presence of a surface reaction. Second, it was hoped that some contribution might be made to the fundamental understanding of carbon monoxide and carbon dioxide chemisorption over this catalyst.

The use of radioactive tracers eliminated any restrictions regarding the linearity of adsorption isotherms.

Information was not extracted from mass peaks, which also

result when tracer samples are injected, primarily because of poor detector sensitivity. The theory which is presented to account for the phenomena observed yielded sparingly to analytical solution. Most of the comparison between theory and experiment was accomplished by numerical solution of the equations resulting when the column was simulated by a series of perfectly mixed tanks.

### I.2 Literature Review

Chromatography was introduced to the world in 1906 by Tswett (53), who used the procedure to separate plant pigments. The column effluent consisted of several zones of different colors, due to the pigments, and as a result Tswett coined the word chromatography, which means "colorwriting," to describe the process. Evidently his work went somewhat unheralded, for it was not until 1941 when the next work in chromatography was published. Martin and Synge (37) introduced the plate theory to partition chromatography and applied it to a liquid-liquid system. James and Martin (25) used a gas as a carrier and thus initiated work in the field of gas chromatography. As the research effort in chromatography began to accelerate, Littlewood et al. (35) used chromatography to calculate heats of solution. Martin (36) suggested the use of gas-liquid partition

chromatography to determine thermodynamic quantities such as interaction potentials.

A number of reviews have been written about chromatography (22, 26, 27, 29, 42). Purnell (42), along with Keulemans (27), was concerned primarily with separation chromatography while Kobayashi et al. (29) concentrated on the use of chromatography in physico-chemical measurements.

Since the mid-1950's a voluminous amount of work has been conducted in chromatography. Most of the work has been concerned with retention volumes or retention times. Stalkup and Kobayashi (47), by measuring retention volumes, determined K values for n-butane in methane-n-decane at high pressure. Stalkup and Kobayashi (46) in a later work confirmed the theory presented in a paper by Stalkup and Deans (45) which predicted N-1 peak velocities for an N component flowing phase infinitesimally perturbed. Koonce et al. (30) demonstrated that a radioactive peak has a different velocity than the concentration peak. Barrere and Deans (4) used chromatography to study absorption with chemical reaction in the carbon dioxide-diethanolamine sys-Eberly (11) applied gas-solid chromatography to the tem. measurement of adsorption isotherms, surface areas, and heats of adsorption at high temperatures.

In a classic paper which stirred interest in peak shape, Van Deemter et al. (55) introduced a relationship

between zone spreading and plate height, which, unfortunately, could not be used  $\underline{a}$  priori to calculate plate height. Giddings (19) introduced the concept of generalized diffusion coefficients which included the kinetic constants of the rate processes involved. Giddings and Seager (21) pointed out that the total variance of a peak could be expressed as the sum of the variances of a number of independent processes. Giddings and Keller (20) qualitatively discussed a slow reversible first order unimolecular reaction under chromatographic conditions for no reaction, intermediate reaction, and complete reaction cases. Klinkenberg (28) analyzed this reaction in a chromatographic column for the latter case and expressed the results in terms of retention time and zone spreading. Kubin (31) and Kucera (33) used LaPlace transforms in solving for expressions for the moments of the eluted peak in gas-solid chromatographic systems. Smith and co-workers (41, 43, 44, 49) combined their results with experimental first and second moments to determine adsorption isotherms, adsorption rate constants, intraparticle diffusion coefficients, surface diffusion coefficients, and axial dispersion coefficients. Aris (2) introduced the moment method, in which the axial distance variable is transformed, by using it to solve the problem of dispersion in capillary flow originally solved by Taylor (50). The moment method has since been used by

Deans et al. (9) to develop a generalized theory of perturbation chromatography in multicomponent systems involving an arbitrary number of chemical reactions. Recently Gangwal et al. (16) applied Fourier analysis to chromatographic peaks.

Carbon monoxide has been observed to adsorb on many solids (1, 5, 12, 13, 14, 15, 17, 18, 24, 32, 34, 39, 51, 58). Eischens and Webb (13) observed the dissociation of carbon monoxide over an iron catalyst, and Ertl (15) observed carbon formation in the carbon monoxide - copper system at high temperatures. Most other work (5, 12, 14) has shown carbon monoxide chemisorption not to be dissocia-Carbon dioxide adsorption in general is not as extensive as that of the monoxide. Unlike the monoxide, carbon dioxide adsorbs both associatively (18, 23, 24, 39, 58) and dissociatively (7, 23, 58). Both carbon oxides have been found to adsorb reversibly on zinc oxide at room temperature (1, 17, 18, 32, 51, 56). Infrared studies (1, 51) on zinc oxide indicated that there exists more than one type of carbon monoxide chemisorption and that surface carbon dioxide exists primarily as a carbonate type structure. Nekipelov and Kasatkina (39) noted that dissociative carbon dioxide adsorption did not occur on their zinc oxide catalyst and were in agreement with Winter (56) in concluding

that the oxygen exchange reaction between carbon monoxide and carbon dioxide was negligible over zinc oxide.

Oxygen exchange between both carbon oxides and catalyst oxygen has been observed over both zinc oxide and cuprous oxides (24, 39, 52). Several investigators (3, 7, 39, 40, 48, 56) have conducted kinetic studies of the oxygen exchange reaction,

$$C*0 + C O_2 \neq C*O_2 + C O$$

where the \* denotes a nonnormal carbon isotope, such as carbon-14. Stroeva et al. (48) measured rate constants for this reaction in the presence of iron oxide, copper, silver, platinum, and cobalt. In spite of the fact that carbon dioxide adsorption on copper oxide at low temperatures is negligible (24, 57), copper was found to catalyze the oxygen exchange reaction in the 250°C - 400°C temperature range. Following the kinetic experiments X-ray analysis of the catalyst indicated that very little of the copper was present as oxide. Cha and Parravano (7) observed this reaction over a titanium dioxide catalyst and concluded that carbon dioxide adsorption was rate limiting.

The copper-zinc oxide catalyst (G-66B) employed in this work was a commercial low temperature shift catalyst. It is generally thought that the catalytic activity for the

water gas shift reaction is provided by the copper, with the zinc oxide playing the role of a support and a spacer to inhibit thermal sintering of the finely dispersed copper (6). Uchida et al. (54) investigated similar copper-zinc oxide catalysts by X-ray and electron microscope techniques. They found the copper to exist primarily in the metallic state and to be of two general types according to structure:

- (1) large massive particles several hundred Å in size, and
- (2) thin patches covering the zinc oxide surface. Musser
- (38) showed that carbon monoxide chemisorption on G-66B was not due exclusively to a one site mechanism, although he was unable to differentiate between various two site mechanisms. A chromatographic study of hydrogen chemisorption was carried out on this catalyst by Suzuki and Smith (49). Their work yielded good adsorption data but no conclusions were reached regarding the mechanism involved.

### II. THEORY

## II.1 General Description

The transient behavior of a slug of tracer being swept down a packed column by a multicomponent carrier gas is to be described. It is assumed that the tracer adsorbs on the surface of the catalyst and may react while on the surface of the catalyst to become a different chemical component. The general mass balance for the tracer in the flowing phase may be written as follows:

$$\frac{\partial c_{i}}{\partial t} + \nabla \cdot c_{i} \overline{u} = \nabla \cdot D\nabla c_{i} + R_{i}$$
 (II-1)

where:  $\overline{u}$  = flowing phase velocity vector

 $c_i$  = concentration of component "i"

D = dispersion coefficient

 $R_i$  = source of component "i" in the flowing phase

Equation (II-1) can be simplified by introduction of the following assumptions:

- (1) Flow is in the axial direction only.
- (2) Flowing phase dispersion is negligible, and therefore D = 0.

The simplified form is

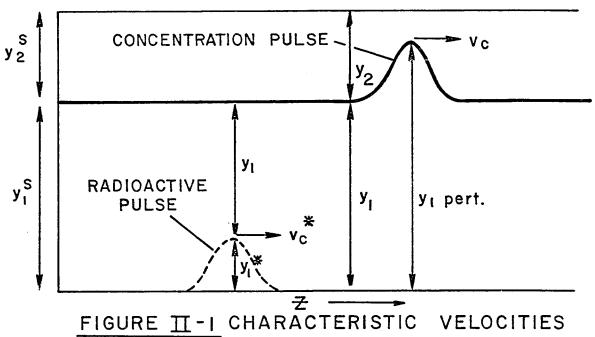
$$\frac{\partial c_{i}}{\partial t} + v \frac{\partial c_{i}}{\partial z} + c_{i} \frac{\partial v}{\partial z} = R_{i}$$
 (II-2)

where: v = average fluid velocity

Collins (8) has shown that for the system to which this theoretical treatment will be applied, injection of a tracer component also results in a concentration disturbance which propagates down the column at a velocity different from that of the tracer. At all points upstream and downstream of this perturbation the total concentration of each chemical component in the carrier gas remains constant at the steady state value that was established before injection of the sample. This is illustrated for a two component system in Figure II-1. Furthermore, Collins' analysis pointed out that the term  $\frac{\partial V}{\partial Z}$  was zero except for certain cases in the region of the perturbation. Therefore, since the tracer will not be at the same location as the concentration perturbation, the term  $\frac{\partial V}{\partial Z}$  can be set equal to zero, and the analysis can be simplified a great deal.

At this point the following assumptions are to be made:

(3) The pressure drop across the column is negligible, so that the pressure can be assumed constant.



- (4) The column is isothermal.
- (5) The flowing phase is an ideal gas mixture.

Introducing these assumptions and setting  $\frac{\partial v}{\partial z}$  equal to zero transforms equation (II-2) as follows:

$$\frac{\partial y_i}{\partial t} + v \frac{\partial y_i}{\partial z} = R_i'$$
 (II-3)

where: y<sub>i</sub> = mole fraction of component "i" in the following phase

$$R_i' = R_i/c$$

c = total molar concentration of the flowing phase

## II.2 Equilibrium Theory

## II.2.1 Generalization

At this point the following assumptions are made:

- (6) All mass transfer and adsorption rates are infinitely fast; i.e., local equilibrium exists.
- (7) Any reactions occurring on the surface are reversible and at equilibrium.

The material balance in the stationary phase is

$$\frac{\partial \mathbf{n}_{i}}{\partial t} = \overline{R}_{i} \tag{II-4}$$

 $\overline{R}_i$  = source of component "i" in the stationary phase

Incorporating assumptions 6 and 7 leads to the following relationship:

$$\overline{R}_{i} = -R_{i}^{!} + \sum_{k} v_{ik} F_{k}$$
 (II-5)

where:  $F_k$  = rate of the kth surface reaction  $v_{ik}$  = the stoichiometric coefficient of component "i" in the kth surface reaction

At this point it becomes necessary to introduce a relationship for the equilibrium existing between the two phases. Such a relation is

$$n_i = \mu_i y_i \tag{II-6}$$

where:  $\mu_i$  = the adsorption equilibrium function of component "i", moles "i" on the surface/mole "i" in the flowing phase and  $\mu_i = \mu_i(T_c, P_c, y_1, y_2, y_3, \dots, y_{n-1}, \text{ catalyst, etc.})$ 

where:  $T_c = column temperature$ 

P<sub>c</sub> = column pressure

y<sub>i</sub> = mole fraction component "i" in the flowing
 phase

n = number of components in the carrier gas

The equilibrium function,  $\mu_{\hat{\mathbf{i}}}$ , can be treated as a constant, since by assumption  $P_{\hat{\mathbf{c}}}$  and  $T_{\hat{\mathbf{c}}}$  are constant and in the vicinity of the tracer peak the total concentrations of distinguishable chemical species are constant.

Combining equations (II-3) through (II-6) yields

$$\frac{\partial y_{i}}{\partial t} + v \frac{\partial y_{i}}{\partial z} + (\mu_{i} \frac{\partial y_{i}}{\partial t} - \sum_{k} \nu_{ik} F_{k}) = 0$$
 (II-7)

# II.2.2 Adsorption Without Reaction

Consider a binary carrier gas consisting of components A and B. Equation (II-7) can be applied to describe the behavior of a tracer component, A\*, which is assumed to be chemically indistinguishable from component A. In this case, since it has been assumed that there is no surface reaction,  $F_k$  = 0. Equation (II-7) becomes for the A-B-A\* system, where 1 and 2 represent components A and B, respectively,

$$(1 + \mu_1) \frac{\partial y_1^*}{\partial t} + v \frac{\partial y_1^*}{\partial z} = 0$$
 (II-8)

where:  $y_i^*$  denotes the isotopic tracer "i".

Equation (II-8), being a hyperbolic partial differential equation, can be solved by the method of characteristics. This method has been well documented with respect to chromatographic systems (4, 8, 38). The characteristic velocity,  $v_{\rm c}^*$ , is given by

$$v_{c}^{*} = \left(\frac{\partial z}{\partial t}\right)_{\dot{y}_{\dot{1}}}^{*} \tag{II-9a}$$

or 
$$v_c^* = -(\frac{\partial y_i^*}{\partial t})/(\frac{\partial y_i^*}{\partial z})$$
 (II-9b)

The solution of equation (II-8), therefore, is

$$v_c^* = \frac{v}{1 + \mu_1}$$
 (II-10)

This can be rearranged to give

$$\mu_1 = (\frac{v}{v_c} - 1)$$
 (II-11)

In terms of more readily obtainable experimental quantities equation (II-11) becomes

$$\mu_1 = (\frac{t_p}{t_r} - 1)$$
 (II-12)

where: t<sub>p</sub> = residence of the peak
t<sub>r</sub> = residence time of the carrier gas

A column conversion constant,  $\beta$ , can be defined as follows:

$$\beta = \frac{m}{V_G c} \tag{II-13}$$

where: m = mass of catalyst in the column  $V_G$  = column free volume

Dividing equation (II-12) by  $\beta$  gives the experimental quantity G\*, which is given in the following equation:

$$G^* = \frac{1}{\beta} \left( \frac{t_p}{t_r} - 1 \right)$$
 (II-14)

and by equation (II-12)

$$G^* = \mu_1^* \tag{II-15}$$

where: 
$$n_{i}^{!} = \mu_{i}^{!} y_{i}$$
 (II-16)

and  $n_i^!$  = moles of component "i"/g catalyst  $\mu_i^!$  = adsorption equilibrium function of component "i",  $\mu_i^!$  =  $\mu_i/\beta$ 

Now consider the addition of a second tracer component,  $B^*$ . A four component system,  $A-B-A^*-B^*$ , now exists and a second equation appears as

$$(1 + \mu_2) \frac{\partial y_2^*}{\partial t} + v \frac{\partial y_2^*}{\partial z} = 0$$
 (II-17)

Since there is no surface reaction  $(F_k = 0)$  equations (II-8) and (II-17) are not coupled, and each can be solved separately by the method of characteristics. The solution to equation (II-17) is

$$G^* = \mu_2' \tag{II-18}$$

## II.2.3 Equilibrium Reaction

Now consider the case of the four component system, A-B-A\*-B\*, under conditions in which the following reaction may be assumed at equilibrium:

$$y_1 y_2^* \qquad y_2 y_1^*$$

where:  $y_i$  = flowing phase mole fraction of component "i"  $y_i^*$  = flowing phase mole fraction of isotopic tracer of "i"

The presence of the above exchange reaction reduces the degrees of freedom for the system from two to one. Because of the coupling effect of the reaction, both tracer components will have the same characteristic velocity as opposed to the case described in Section II.2.2. For the tracer components, equation (II-7) becomes

$$\frac{\partial y_1^*}{\partial t} + v \frac{\partial y_1^*}{\partial z} + \mu_1 \frac{\partial y_1^*}{\partial t} - F^* = 0$$
 (II-19a)

$$\frac{\partial y_2^*}{\partial t} + v \frac{\partial y_2^*}{\partial z} + \mu_2 \frac{\partial y_2^*}{\partial t} + F^* = 0$$
 (II-19b)

where: F\* = the rate of the exchange reaction

The form of the equilibrium constant for the exchange reaction is assumed to be

$$K = \frac{y_1^* y_2}{y_2 y_1}$$
 (II-20a)

or 
$$\frac{y_1^*}{y_2^*} = K \frac{y_1}{y_2}$$
 (II-20b)

Combining equation (II-20b) with

$$y_{i}^{s} = y_{i}^{*} + y_{i}$$
 (II-21)

where:  $y_i^s$  = the steady state mole fraction of component "i" yields

$$\frac{y_1^*}{y_2^*} = K \frac{y_1^s}{y_2^s}$$
 (II-22)

That is, in the vicinity of the tracer pulse, the ratio of the tracer components is constant. With this restriction, equation (II-19a) can be multiplied by  $(1/y_1^*)$  and added to the product of equation (II-19b) and  $(-1/y_2^*)$  to give

$$F^* = \frac{y_2^{\mu_1} \frac{\partial y_1^*}{\partial t}}{y_1^{\mu_1} + y_2^{\mu_2}} - \frac{y_1^{\mu_2} \frac{\partial y_2^*}{\partial t}}{y_1^{\mu_2} + y_2^*}$$
(II-23)

Equation (II-23) can be rearranged by using equation (II-22) as follows:

$$F^* = \frac{\frac{y_1}{2}}{1 + \frac{K y_1^s}{y_2^s}} - \frac{\frac{y_2}{2}}{1 + \frac{y_2^s}{K y_1^s}}$$
(II-24)

Substitution of equation (II-24) into equation (II-19a) results in

$$\frac{\partial y_{1}^{*}}{\partial t} + v \frac{\partial y_{1}^{*}}{\partial z} + \frac{K_{\mu_{1}} y_{1}^{s} \frac{\partial y_{1}^{*}}{\partial t}}{y_{2}^{s} + K y_{1}^{s}} + \frac{K y_{1}^{s} \mu_{2} \frac{\partial y_{2}^{*}}{\partial t}}{K_{1} y_{1}^{s} + y_{2}^{s}} = 0 \quad \text{(II-25)}$$

Using equation (II-22) to convert the last term of equation (II-25) gives

$$\frac{\partial y_{1}^{*}}{\partial t} \left(1 + \frac{K_{\mu_{1}} y_{1}^{s} + \mu_{2} y_{2}^{s}}{K y_{1}^{s} + y_{2}^{s}}\right) + v \frac{\partial y_{1}^{*}}{\partial z} = 0$$
 (II-26)

Once again solving by the method of characteristics gives as the solution to equation (II-26)

$$G^* = \frac{K\mu_1' y_1^s + \mu_2' y_2^s}{K y_1^s + y_2^s}$$
 (II-27)

The addition, then, of an equilibrium reaction in the four component system, A-B-A\*-B\*, results in reducing the number of tracer peaks from two to one, with the subsequent value of G\* resulting in a linear combination of the G\* values to be expected when there is no reaction.

## II.3 Nonequilibrium Theory

In Section II.2 equation (II-3) was applied to cases in which all adsorption and reaction rate processes were either sufficiently rapid to be assumed at equilibrium or slow enough to be neglected. At the intermediate stages, where neither of these assumptions is valid, the equations can no longer be put in the hyperbolic form. The equations can be solved numerically, however, by simulating the column by a series of perfectly mixed tanks according to the method

of Deans and Lapidus (10).

As explained in Section II.2.3 the coupling is provided by the exchange reaction. If the isotopic tracers are assumed to be infinitely dilute, the mole fractions of A and B can be assumed to be constant and equal to the steady state mole fractions. The exchange reaction can then effectively be written as

$$B^* \stackrel{\Rightarrow}{\leftarrow} A^*$$

$$y_2^* y_1^*$$

Following equation (II-20a), the equilibrium can be expressed as  $\frac{1}{2}$ 

$$(\frac{y_1^*}{y_2^*}) = K'$$
 (II-28)

where: 
$$K' = K \frac{y_1^s}{y_2^s}$$
 (II-29)

In general it must be assumed that both adsorption and reaction processes may not be at equilibrium. In such a case the two tracer components can be described by equation (II-3) as follows:

$$\frac{\partial y_1^*}{\partial t} + v \frac{\partial y_1^*}{\partial z} - R_1^* * = 0$$
 (II-30a)

$$\frac{\partial y_2^*}{\partial t} + v \frac{\partial y_2^*}{\partial z} - R_2^{!*} = 0$$
 (II-30b)

Equations (II-30) could be placed in the form of equation (II-7) if it could be assumed that all the adsorption processes were at equilibrium.

The exact form of R<sub>1</sub>\* and R<sub>2</sub>\* depends on the mechanism chosen to explain the adsorption and reaction phenomena. Equations (II-30) can be rewritten for each tank "j" used in modeling the column as follows:

$$\frac{d y_1^*(j)}{d\tau} = y_1^*(j-1) - y_1^*(j) + \frac{v_t R_1^{'*}(j)}{Q}$$
 (II-31a)

$$\frac{d y_2^*(j)}{d\tau} = y_2^*(j-1) - y_2^*(j) + \frac{v_t R_2^{'*}(j)}{Q}$$
 (II-31b)

where: 
$$\tau = \frac{t}{V_t}$$
 (II-32)

and 
$$V_t = V_G/N$$
 (II-33)

where: Q = column flow rate

 $V_t$  = volume of each tank

N = number of tanks used to simulate the column

II.4 The CO - 
$$CO_2$$
 -  $C^{14}O$  -  $C^{14}O_2$  System

### II.4.1 General

An interesting practical example of the theoretical three and four component systems discussed in Sections II.2 and II.3 is the mixture consisting of carbon monoxide and carbon dioxide and one or both of their respective carbon-14 isotopes in the presence of a Cu-ZnO water gas shift catalyst. The impetus to investigate this system stems from the fact that the catalyst is commercial and in common It is of interest therefore to attempt to understand usage. the surface chemistry involved with this catalyst and the carbon oxides, which are two of the four major chemical species involved in the water gas shift reaction. Musser (38) has investigated carbon monoxide adsorption and the oxygen exchange reaction between carbon monoxide and carbon dioxide over this catalyst. The oxygen exchange reaction can be written as

$$c_0 + c_{2}^{14} + c_{2} \stackrel{?}{\leftarrow} c_{14} + c_{2}$$
 $y_1 \quad y_2 \quad y_1 \quad y_2$ 

Musser found that by varying the flow rate the extent of the exchange reaction could be controlled. For high flow rates in a short column, it might reasonably be assumed that the exchange reaction is negligible. Under such conditions, the retention of each tracer may be expressed according to equations (II-15) and (II-18) as follows:

$$G^* = \mu_{C0}^{\prime} \tag{II-34a}$$

$$G^* = \mu_{C0}^{\dagger} \qquad (II-34b)$$

For the opposite situation, in which there are low flow rates in long columns, it is assumed that the exchange reaction is at equilibrium. It is further assumed that the equilibrium constant, K, for this reaction is equal to unity. According to equation (II-27), then, and using the fact that  $\sum_{i=1}^{\infty} y_{i} = 1$ , the relationship for G\* is

$$G^* = \mu_{C0}^{\prime} y_{C0}^{s} + \mu_{C0}^{\prime} y_{C0}^{s}$$
 (II-35)

## II.4.2 The Mechanism

Musser (38), in his brief look at this reaction, attempted unsuccessfully to explain his data in terms of a single surface reaction coupling two surface species. The mechanism shown on the following page was advanced to explain the reaction and adsorption phenomena observed on

this catalyst. Since dissociative adsorption on metals is not uncommon (24), it was assumed that a dissociative carbon dioxide adsorption step was the key to the exchange reaction. The basis for assuming this five step mechanism is presented in Section IV.1.2.

3. 
$$C0_2 + B \stackrel{?}{\leftarrow} C0_2$$

5. 
$$C0_2 + C \stackrel{?}{\leftarrow} C0_2$$

The assumed equilibrium relationships are as follows:

$$K_{1} = \frac{n_{C0}^{A}}{y_{C0}^{A}}$$
 (II-36a)

$$K_2 = \frac{n_{C0}^B}{y_{C0}^B}$$
 (II-36b)

$$K_3 = \frac{n_{C0}^B}{y_{C0_2}^B}$$
 (II-36c)

$$K_4 = \frac{n_{C0}^B n_0^B}{n_{C0}^B}$$
 (II-36d)

$$K_{5} = \frac{n_{C0_{2}}^{C}}{y_{C0_{2}}^{C}}$$
 (II-36e)

where:  $n_{i}^{M}$  = surface concentration of component "i" on site "M"

A,B,C = concentration of unoccupied type A, B, C, adsorption sites, respectively, moles of site/mole flowing phase

and 
$$A = \frac{A_z}{1 + K_1 y_{C0}}$$
 (II-37a)

$$B = \frac{B_z}{1 + K_2 y_{C0} + K_3 y_{C0} + \frac{K_3 K_4}{K_2} \frac{y_{C0}}{y_{C0}}}$$
 (II-37b)

$$C = \frac{C_z}{1 + K_5 y_{C0_2}}$$
 (II-37c)

where:  $A_z$ ,  $B_z$ ,  $C_z$  = total site concentrations of type A, B, C, respectively, mole site/mole flowing phase It should be pointed out that since in the vicinity of the tracer the total concentration of each distinguishable chemical component is constant, the quantities A, B, C and  $\mathbf{n}_0^B$  are constant for a given carrier gas.

Equations (II-36) can be placed in the form of equation (II-6) as follows:

$$\mu_{C0}^{A} = n_{C0}^{A}/y_{C0}$$
 (II-38a)

$$\mu_{C0}^{B} = n_{C0}^{B}/y_{C0}$$
 (II-38b)

$$\mu_{C0_2}^B = n_{C0_2}^B / y_{C0_2}$$
 (II-38c)

$$K_4' = n_{C0}^B / n_{C0}^B$$
 (II-38d)

$$\mu_{C0_2}^C = n_{C0_2}^C / y_{C0_2}$$
 (II-38e)

where:  $\mu_{i}^{M}$  = the adsorption equilibrium function of component "i" on site "M"

K'<sub>4</sub> = surface chemical equilibrium function, mole B
type CO/mole B type CO<sub>2</sub>

# II.4. Application of the Equilibrium Theory

Since the mechanism proposes two types of adsorption

for carbon monoxide, the following expression can be written:

$$n_{C0} = n_{C0}^{A} + n_{C0}^{B}$$
 (II-39a)

and, therefore

$$\mu_{C0} = \mu_{C0}^{A} + \mu_{C0}^{B}$$
 (II-39b)

Equation (II-34a) describes the situation in which both types of adsorption are near equilibrium. Now consider the case in which type B carbon monoxide adsorption is negligibly slow. In this case equation (II-15) becomes

$$G^* = \mu_{C0}^{A^{\dagger}} \tag{II-40}$$

Similarly, for the carbon dioxide, assuming step 3 to always be rapid while step 5 is negligible, equation (II-18) becomes

$$G^* = \mu_{CO_2}^{B'} \qquad (II-41)$$

Accordingly, there are two subcases when the exchange reaction is at equilibrium, depending on whether or not step 5 is included. If this carbon dioxide adsorption step can be neglected, equation (II-35) is modified to

become

$$G^* = \mu_{C0}^* y_{C0}^s + \mu_{C0}^{B^*} y_{C0}^s$$
 (II-42)

On the other hand, if all five steps of this mechanism can be assumed to be near equilibrium, equation (II-35) remains unchanged.

$$G^* = \mu_{C0}^{\dagger} y_{C0}^{s} + \mu_{C0}^{\dagger} y_{C0}^{s}$$
 (II-35)

## II.4.4 The Nonequilibrium Treatment

For the regions in which nonequilibrium processes cannot be neglected, the coupled equations can be solved numerically as explained in Section II.3. The rate equations for the five steps are as follows:

$$r_1 = k_1 A(y_{C0}^* - n_{C0}^{A*}/\mu_{C0}^A)$$
 (II-43a)

$$r_2 = k_2 B(y_{C0}^* - n_{C0}^{B*}/\mu_{C0}^B)$$
 (II-43b)

$$r_3 = k_3 B(y_{C0_2}^* - n_{C0_2}^{B*}/\mu_{C0_2}^B)$$
 (II-43c)

$$r_4 = k_4 B(n_{C0_2}^{B*} - n_{C0}^{B*}/K_4')$$
 (II-43d)

$$r_5 = k_5 C(y_{C0_2}^* - n_{C0_2}^{C*}/\mu_{C0_2}^C)$$
 (II-43e)

where:  $r_{\ell}$  = rate of step "\ell", dimensionless  $k_{\ell}$  = rate constant of step "\ell", dimensionless

The source terms,  $\frac{V_t R_1'^*(j)}{Q}$  and  $\frac{V_t R_2'^*(j)}{Q}$ , in equations (II-31) can now be expressed as follows:

$$\frac{V_t R_1'^*(j)}{Q} = -r_1(j) - r_2(j)$$
 (II-44a)

$$\frac{V_t R_2^{!*}(j)}{Q} = -r_3(j) - r_5(j)$$
 (II-44b)

Equations (II-31) now become

$$\frac{d \ Y_{C0}^{*}(j)}{d\tau} = y_{C0}^{*}(j-1) - y_{C0}^{*}(j) - r_{1}(j) - r_{2}(j)$$

$$\frac{d \ y_{C0_{2}}^{*}(j)}{d\tau} = y_{C0_{2}}^{*}(j-1) - y_{C0_{2}}^{*}(j) - r_{3}(j) - r_{5}(j)$$
(II-45b)

The rate equations for the four surface species are

$$\frac{d n_{C0}^{A*}}{d\tau} = r_1(j)$$
 (II-46a)

$$\frac{d n_{C0}^{B*}}{d\tau} = r_2(j) + r_4(j)$$
 (II-46b)

$$\frac{d n_{C0_2}^{B*}}{d\tau} = r_3(j) - r_4(j)$$
 (II-46c)

$$\frac{d n_{C0}^{C*}}{d\tau} = r_5(j)$$
 (II-46d)

#### III. EXPERIMENTAL

## III.1 Equipment

The equipment, along with the direction of gas flow, is depicted schematically in Figure III-1. Carbon monoxide-carbon dioxide and helium-carbon dioxide carrier gas mixtures were prepared in standard 1A gas cylinders. Refer to Appendix D for details. As shown, the system could accommodate as many as three gas cylinders. Since the helium, used for catalyst activation and free volume determinations, and the hydrogen, used for activation, were never disconnected, changing carrier composition required physically interchanging cylinders.

Upon expansion through a two stage pressure regulator, the gas passed first through a filter and then through a flow controller on its way to the precolumn, which was housed in the oven. The role of the precolumn was to remove any poisons which might be present in the feed stream. The sampling valve was located immediately downstream from the reference side of the thermal conductivity cell. An injected sample passed directly into the oven and hence the test column. Upon exiting the test column and the oven,

## Numerical Legend

## Figure III-1

- 1. Hydrogen
- 2. Helium
- 3. Carrier Gas
- 4. Pressure Regulator
- 5. Filter
- 6. Pressure Gage
- 7. Metering Valve
- 8. Flow Controller
- 9. Precolumn
- 10. Test Column Assembly
- 11. Sampling Valve
- 12. Thermal Conductivity Cell
- 13. Bridge
- 14. Ionization Chamber
- 15. Preamplifier
- 16. Electrometer
- 17. Recorder
- 18. Soap Bubble Meter
- 19. Oven

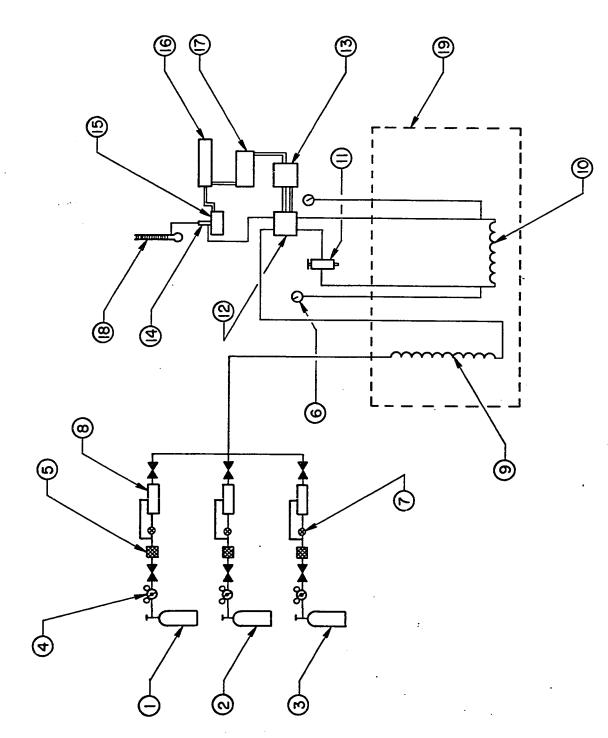


FIGURE III-1 SCHEMATIC FLOW DIAGRAM

the concentration peak was monitored in the sample side of the thermal conductivity cell. The effluent of the thermal conductivity cell entered the ionization chamber, where the radioactive tracer concentration was measured. The outputs of both detectors were recorded on a two channel chart recorder. The gas then exited through a 50 cc soap bubble flow meter to the hood, which exhausted to the atmosphere. Only the columns were thermostated; the remainder of the equipment was exposed to room conditions.

Two test columns were required in order to procure data over the desired range of residence times. Previous investigators (4, 38) used a capillary bypass, having a negligible residence time, to obtain a reference peak and thus eliminate the need to calibrate the system for lag time caused by dead volume and finite instrumentation responses. For experiments in which it was desired to maintain the residence time of the gas flowing through the column at a low value, the procedure resulted in unacceptably poor resolution of the two peaks. Therefore, the design shown in Figure III-2 was employed to overcome this problem. By interchanging line 1 and line 2 connections, flow could be directed either through the two columns in series or through the short column alone. In this manner the catalyst in both the short column and the long column had the same activation and temperature history. The bypass

# Numerical Legend Figure III-2

- 1. Short Column Entrance
- 2. Long Column Entrance
- 3. Plug
- 4. Oven
- 5. Short Column
- 6. Long Column
- 7. Pressure Gage
- 8. Toggle Valve
- 9. Bypass Line (for short column)
- 10. Bypass (for columns in series)

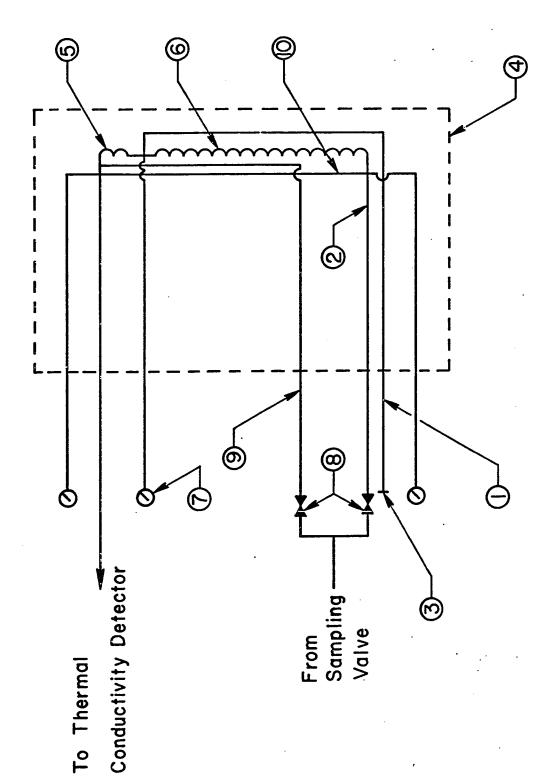


FIGURE III-2 TEST COLUMN ARRANGEMENT

could be used when the two columns were connected in series. When only the short column was in use, manipulation of the toggle valves directed flow either through the column or by the column. Therefore, the bypass and reference peaks could be obtained separately.

Pressure gages were used to measure column entrance and exit pressures, all of which were close to atmospheric. Mercury manometers were avoided because of the possible effects of the mercury vapor on the activity of the catalyst. The system could be evacuated on both sides of the precolumn and downstream of the test column.

A sample manifold, shown in Figure III-3, was constructed so that radioactive samples could be diluted and expanded into the sample loop for injection. An argon supply was connected to the manifold for free volume determinations. Details of the sample system can be found in Appendix C.

### III.2 Procedure

Following activation, helium was passed over the catalyst in order to carry out bypass and free volume calibrations for both the long (series) and short columns.

Upon completion of this procedure, a carbon monoxide-carbon dioxide carrier gas mixture of the desired concentration

## Numerical Legend

## Figure III-3

- 1. Stopcock
- 2. Breakseal
- 3. Ballbearing
- 4.  $C^{14}O_2$  Supply
- 5. C<sup>14</sup> O Supply
- 6. 30 cc Sample Container
- 7. Pressure Gage
- 8. Sampling Valve
- 9. Kovar Seal
- 10. Vacuum Pump
- 11. Sample Loop
- 12. External Inlet For Argon and Diluting Gases

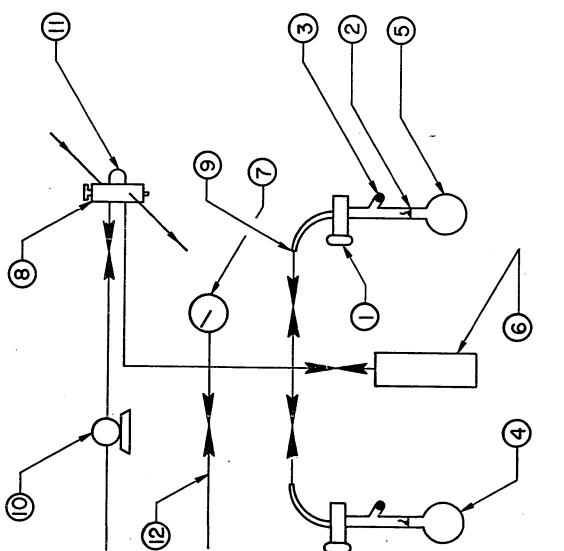


FIGURE III - 3 SAMPLE SYSTEM

was allowed to flow slowly overnight over the catalyst in the long column. This procedure insured that any initial rapid catalyst deactivation was completed; and it allowed any helium, hydrogen, or water vapor trapped in dead ends, such as pressure gage connections, to diffuse outward. Experiments were then ready to be carried out in the long column.

The flow rate was established by opening the metering valve to the appropriate setting. When the thermal conductivity cell output indicated that the system had reached equilibrium, the flow rate was measured via the soap bubble Simultaneously, oven temperature, inlet and outlet column pressures, room temperature, and barometric pressure were recorded. After the appropriate recorder range and chart speed were verified, carbon monoxide tracer was expanded into the sample manifold to a pressure of about 25" Hg vacuum. This pressure varied somewhat depending on the relative strength of the supply and the residence time of flow through the column. The sample then was injected via the sampling valve and the response was observed on the recorder. Since the long column (series configuration) was in use the output consisted of two peaks, the first due to the bypass and the second due to the column. The time elapsed between these peaks was treated as the residence time of the peak in the column. Determination of the peak

first moments is discussed in Appendix D.

After both tracers had been observed under these conditions, the metering valve was reset, and a new flow rate was established. The same data acquisition and sampling procedure was repeated.

For the high range of flow rates, the chromatographic train was reconnected so that experiments could be conducted over the short column. The experimental range of flow rates was limited by excessive pressure drop on the high end and by the minimum obtainable flow rate on the low end. The latter was determined by the flow controller capability and flow measurement accuracy.

For the short column, the procedure had to be modified slightly, however, because the bypass peak and the column peak had to be recorded separately as described earlier. The toggle valves first were positioned so that flow bypassed the column. After equilibrium conditions were attained, a sample of either tracer was expanded into the manifold. It was now necessary to mark the time of injection. This was accomplished by switching the chart movement switch to the off position and marking the pen position. Then, the chart movement switch was turned on simultaneously with injection of the sample. With the bypass peak thus recorded, the two toggle valve positions were reversed. When steady state was indicated, the same

set of data as described before was taken. Two samples were injected, one of each tracer, and the injection times were marked by the same procedure used for the bypass peak. As with the long column, flow rates were varied over a range with column and bypass samples being injected and data recorded at each point.

Upon completion of studies with a particular composition carrier gas, another mixture was investigated. The system was converted to the long column configuration and the new mixture was allowed to pass over the catalyst overnight. From this point the experimental procedure becomes identical with that already described for the first carrier gas.

Experiments with the helium-carbon dioxide carrier gas mixtures were abbreviated considerably with respect to the studies described previously. All data were taken at the same flow rate for the various mixtures. The work was conducted on the long column.

## IV. RESULTS AND CONCLUSIONS

# IV.1 Carbon Monoxide - Carbon Dioxide System

## IV.1.1 Experimental Results

As was explained in Section III.2 the retention of both carbon monoxide and carbon dioxide tracers at  $400^{\circ}F$  and atmospheric pressure was recorded as a function of carrier gas residence time,  $t_r$ , for each carrier gas mixture. For each chromatogram the centroids of the bypass and main peaks were approximated by the procedure described in Appendix D. The difference between these two values was taken to be the residence time of the tracer in the column,  $t_p$ . This value was normalized to the flow rate by converting to the retention quantity G\* according to equation (II-14).

$$G^* = \frac{1}{\beta} \left( \frac{t_p}{t_r} - 1 \right)$$
 (II-14)

The purpose of  $\beta$  is to give G\* units of moles/g catalyst.

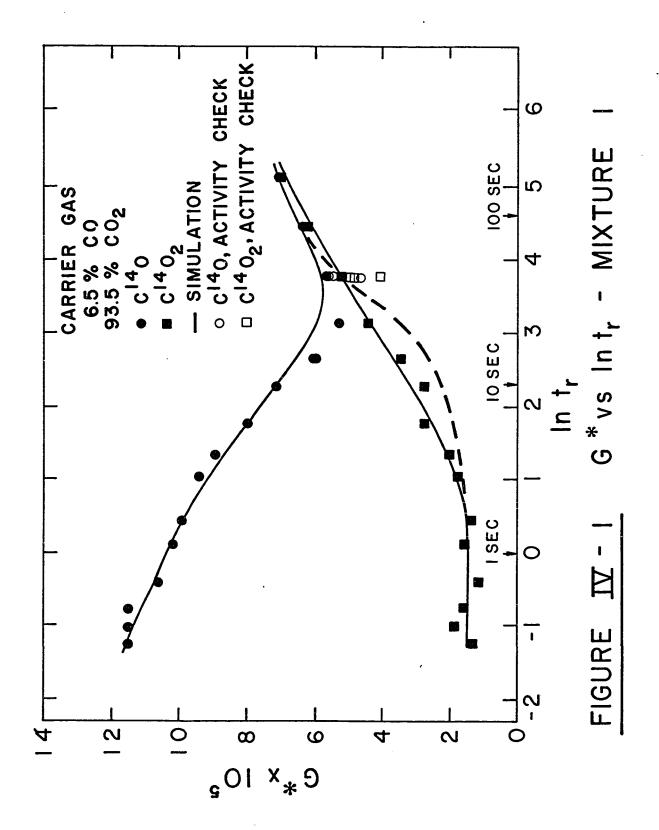
The experimental and calculated results for the carbon monoxide - carbon dioxide runs are tabulated in Appendices G and H, respectively. The results are plotted

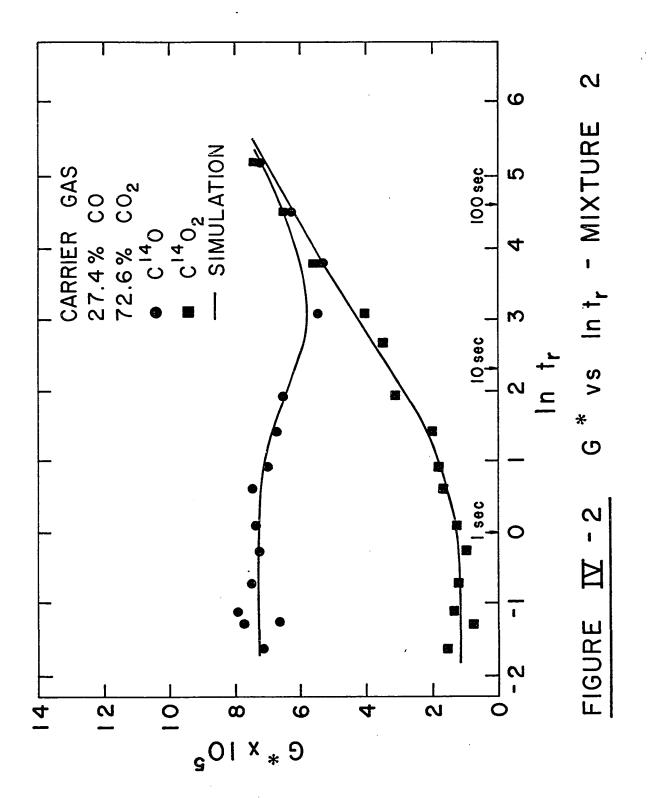
in terms of  $G^*$  versus  $ln\ t_r$  in Figures IV-1 through IV-7. These data are the basis for this thesis.

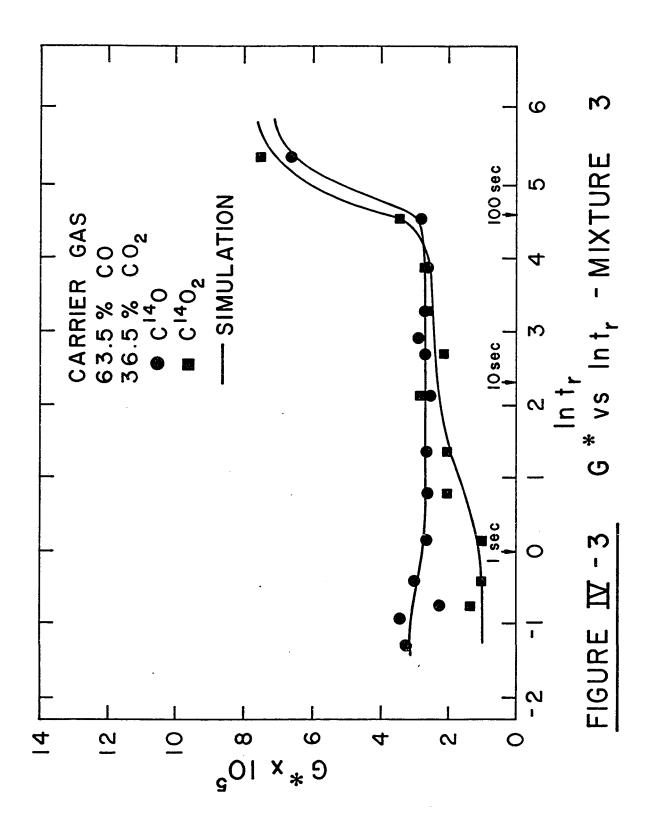
The numbering of the carrier gas mixtures reflects the chronological order in which the experiments were conducted. Table C-1 lists the compositions of all carrier gases used in this work.

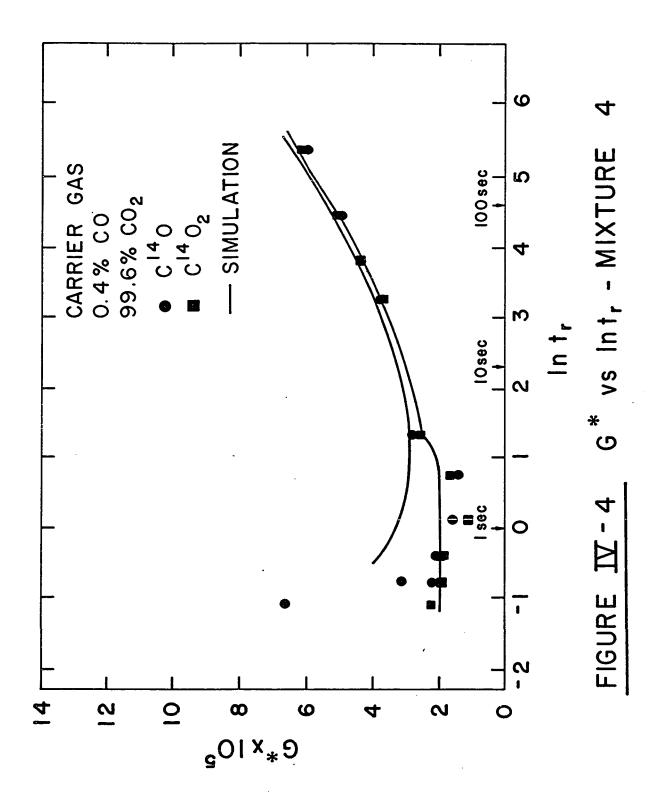
Originally it was hoped that by varying the residence time of the carrier gas (i.e., the velocity for a given column), it would be possible to define two distinct regions of behavior. This was based on the assumption that the surface exchange reaction step was a considerably slower process than either carbon monoxide or carbon dioxide adsorption on this catalyst. One region, corresponding to large values of t<sub>r</sub>, would be characterized by the existence of adsorption and reaction processes all being at equilibrium. Within the limits of the other region, at low t<sub>r</sub> values, the exchange reaction would be negligibly slow while the adsorption steps would remain essentially at equilibrium.

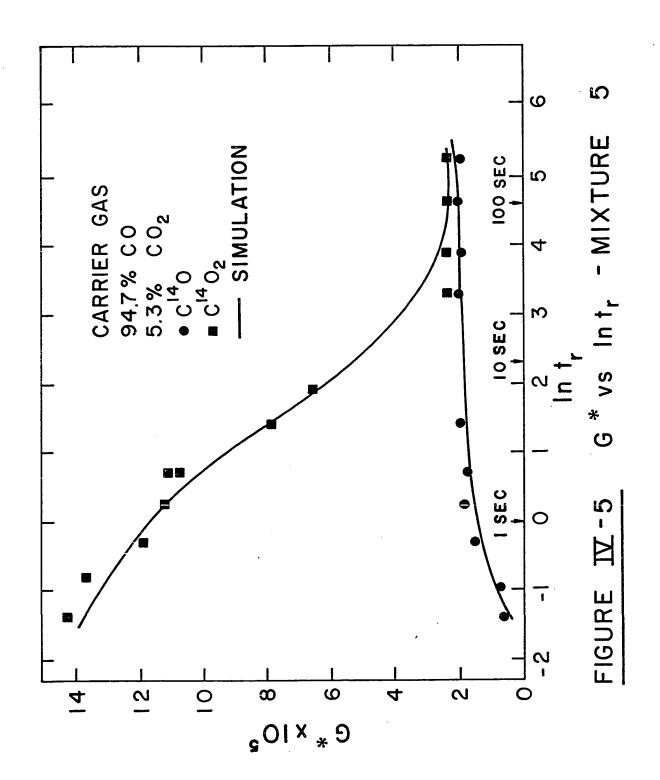
This approach met with little success, however, being too much of an oversimplification. As can be seen, the data generally are characterized by nonequilibrium processes; the existence of plateaus of constant G\* is more the exception than the rule. Regions in which the equilibrium theory presented in Sections II.4.1 and II.4.3 is

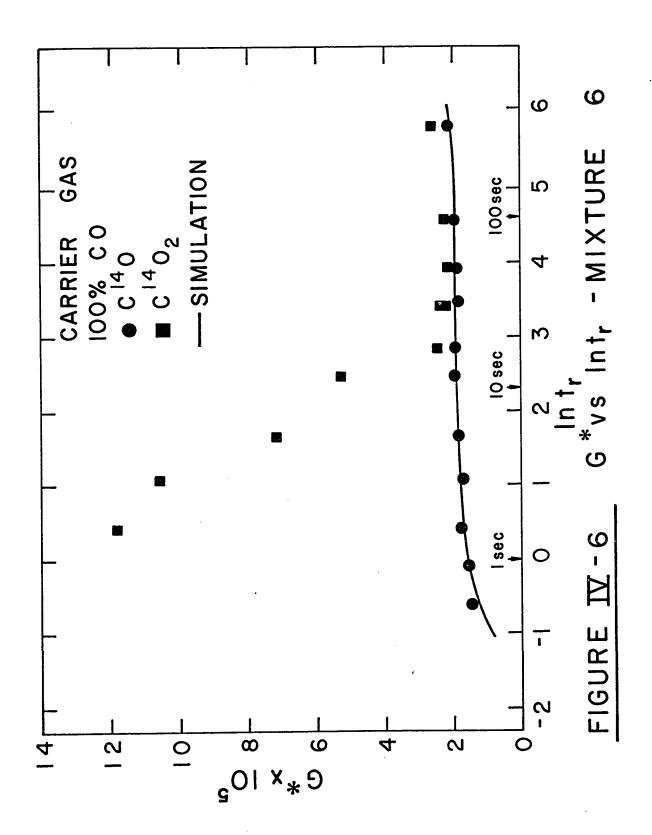


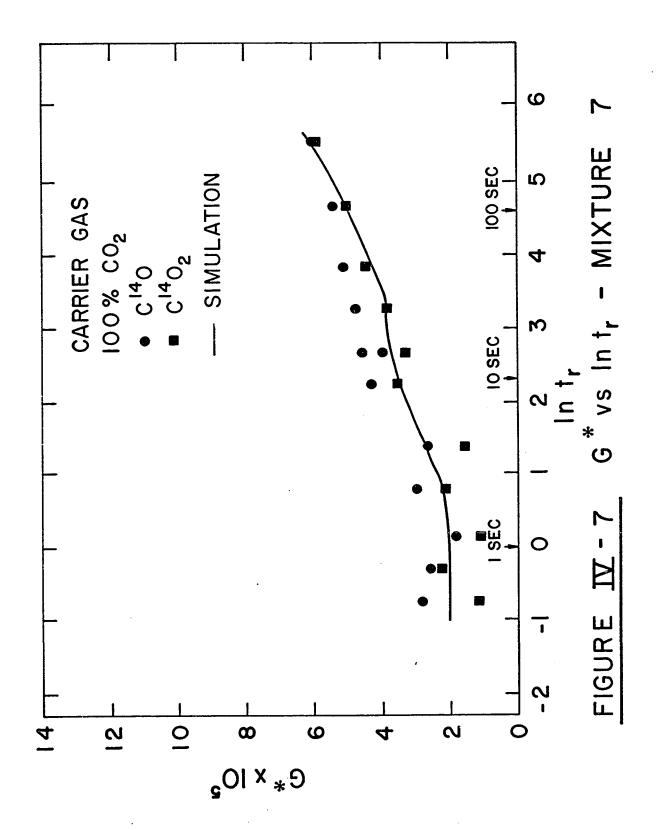












valid will be pointed out in Section IV.1.3.

Qualitatively, several interesting features can be observed in Figures IV-1 through IV-7. In mixtures 1, 2, 4, and 7, which are rich in carbon dioxide, a slow adsorption process is evident because G\* continues to increase even after the exchange reaction has apparently reached In mixtures 2 and 3 the retention of the carbon dioxide tracer at low t<sub>r</sub> values is less than the carbon monoxide tracer; but as  $t_r$  becomes larger the carbon dioxide tracer eventually is retained longer than the carbon monoxide. This indicates that the slow adsorption process is a carbon dioxide step. Data taken with mixtures 3 and 5 also indicate that this slow carbon dioxide adsorption step is not necessary for the oxygen exchange reaction It is also evident that as the carbon monoxide concentration in the carrier gas increases this carbon dioxide step becomes even slower until for mixture 5, it is beyond the range of experimental investigation. Contrasting the previously described type of adsorption is a fast form of carbon dioxide adsorption which is present at all seven carrier gas compositions.

Carbon monoxide, on the other hand, appears to adsorb rapidly in all cases except mixtures 5 and 6, in which at  $t_r$  values less than one second the G\* value for the

carbon monoxide tracer appears to decrease.

## IV.1.2 Column Simulation

As was pointed out in Section IV.1.1, the data generally were characterized by nonequilibrium processes, which invalidated the assumptions leading to the solutions to the equations presented in Sections II.4.1 and II.4.3. It was necessary to solve the rate equations numerically in order to describe the data over the entire range of  $t_r$ .

The column was simulated by a number of perfectly mixed tanks in series according to the method of Deans and Lapidus (10). A copy of the Fortran program is included in Appendix I. In this system the column dispersion amounted to only a small fraction of the dispersion created by the kinetic processes involved. As a result it was possible to reduce the number of tanks used to approximate the column to thirty without affecting the results. This was checked several times by using 45 and 60 tanks. The output in each case was unchanged. The retention time of the simulated peak was determined by the same method used for the experimental peaks; that is, the centroid of each peak was approximated by the procedure described in Appendix D instead of using the peak maximum as a time reference.

Several mechanisms advanced to describe the adsorption processes in this system were found to be unsatisfactory.

The five step scheme presented in Section II.4.2 proved to explain the data where the others failed. This is not to say that this mechanism is a unique description of the system. It does, however, combine simplicity with qualitative agreement. Three adsorption steps and a reaction step were pointed out in Section IV.1.1. The fifth step had to be added in order to simulate the data satisfactorily.

It was originally hoped that the constants  $K_{\ell}$  and  $k_{\ell}$ , in equations (II-36) and (II-43), respectively, would fit the data over the entire range of carrier gas compositions. After three sets of data (carrier gas mixtures) had been roughly fit, it became obvious that  $K_{\ell}$  and  $k_{\ell}$  were not constant over the entire range of carrier gas compositions. Therefore, the data for each mixture were fit according to the following modified version of the mechanism presented in Section II.4.2.

- 1.  $C0 \stackrel{?}{\leftarrow} (C0)_A$
- 2.  $C0 \stackrel{?}{\leftarrow} (C0)_B$
- 3.  $C0_2 \stackrel{?}{\leftarrow} (C0_2)_B$
- 4.  $X + (C0_2)_B \stackrel{?}{\leftarrow} (C0)_B + X0$
- 5.  $C0_2 \stackrel{?}{\leftarrow} (C0_2)_C$

where: X = any oxygen acceptor  $(i)_M$  = component "i" on site "M" The equilibrium functions in the above kinetic scheme remain identical to those listed in equations (II-38). The rate parameters,  $k_{\ell}$ , for the above steps become, in terms of those in equations (II-43)

$$k_1^{\dagger} = k_1 A \qquad (IV-1a)$$

$$k_2^* = k_2 B \tag{IV-1b}$$

$$k_3' = k_3 B \tag{IV-1c}$$

$$k_4' = k_4 \tag{IV-1d}$$

$$k_5' = k_5 C (IV-1e)$$

There are some subtle differences between this scheme and the mechanism presented in Section II.4.2 which merit discussion. In step 4, which provides the coupling between the two tracers, it now becomes impossible to distinguish between a direct oxygen transfer process and the dissociation of molecularly adsorbed carbon dioxide. It is also no longer possible to differentiate between sites "A" and "C". That is, the carbon monoxide and carbon dioxide adsorption processes, steps 1 and 5, which are not involved directly in the surface exchange reaction may or may not occur on the same sites.

Perhaps the most interesting difference between the two mechanisms is that the former assumes Langmuir behavior and the latter does not. One of the assumptions on which the Langmuir adsorption model is based is that the surface is energetically uniform. This is often quite unrealistic, and the results of Section IV.2.2 demonstrate this with respect to carbon dioxide adsorption on this catalyst.

As stated earlier, no one set of constants could be found which fit all the data. For this reason no attempt was made to use statistical methods to minimize the error between the simulated results and the experimental data. The fact that quantitative agreement can be achieved is apparent from Figures IV-1 through IV-7. It should be pointed out that for carbon dioxide tracer in pure carbon monoxide carrier gas, numerical simulation was not possible because the equilibrium function for the surface reaction step becomes infinite. Simulation was also not possible in the opposite case, carbon monoxide tracer in carbon dioxide carrier gas, because the surface reaction equilibrium function equals zero. Consequently, the last term in equation (II-43d) becomes infinite.

The results of the numerical studies indicated that some of the adsorption processes were, in fact, more rapid than others. Table IV-1 gives a qualitative classification

of five kinetic steps according to relative speed.

TABLE IV-1 Relative Rates of the Various Steps

Step 1	Carbon monoxide adsorption	fast
Step 2	Carbon monoxide adsorption	slow
Step 3	Carbon dioxide adsorption	fast
Step 4	Surface reaction	moderate
Step 5	Carbon dioxide adsorption	slow

Equilibrium and rate parameters in equations (II-38) and (IV-1) used to account for the results in Figures IV-1 through IV-7 are shown in Table IV-2. The equilibrium constant  $K_4^*$  is omitted because, as is shown in Appendix A, it is not an independent variable. Once again it should be emphasized that these numbers are of a qualitative significance only. In some cases the results were insensitive to certain of the parameters. The numbers used in these cases are not to be taken seriously.

Contradicting the hypothesis advanced in Section IV.1.1, the results of this study show that the surface reaction is not the slowest step. One of the types of both carbon monoxide and carbon dioxide adsorption is apparently slower than step 4. An interesting consequence is that

TABLE IV-2 Equilibrium and Rate Parameters<sup>†</sup>

Mixture	7	4	1	2	3	5	6
$^{\mu}_{ extsf{C0}}^{ extsf{A}}$	6.0	6.0	4.87	3.34	1.3	0.73	0.87
$^{\mu}_{ extsf{C0}}^{ extsf{B}}$	208.*	208.*	13.0	3.34	0.22	0.34	0.36
$^{\mu}^{B}_{\text{CO}_{2}}$	0.84	0.84	0.67	0.57	0.47	0.1*	u
<sup>C</sup> C0 <sub>2</sub>	1.34	1.34	1.44	1.38	6.96	u	u
$\frac{Q k_1^t}{V_t} (sec)^{-1}$	e	e	e	е	e	4.0	5.3
$\frac{Q k_{2}^{\prime}}{V_{t}} (sec)^{-1}$	е	e	0.22	.096	0.21	.011	.013
$\frac{Q k_3'}{V_t} (sec)^{-1}$	e	e	e	е	e	е	e
$\frac{Q k_{4}^{t}}{V_{t}} (sec)^{-1}$	0.43	0.43	0.60	0.55	0.90	е	u
$\frac{\frac{Q k_{5}^{\prime}}{V_{t}}(sec)^{-1}}{V_{t}}$	.017	.017	.021	.016	.063	u	u

<sup>&</sup>lt;sup>†</sup>The equilibrium parameters in Table IV-2 can be converted to the form of equation (II-15) by dividing by β. Although, strictly speaking, β varies with the flow rate, i.e., with the pressure drop, an approximate value for β is 0.43 x 10<sup>5</sup> g/g mole.

<sup>\*</sup>Denotes that the simulation was insensitive to this parameter.

eDenotes that the rate parameter was set sufficiently high to insure equilibrium at all times.

UDenotes that this step was unnecessary to explain the data, so the rate constant was set at zero.

carbon monoxide adsorption, step 2, is the rate limiting step for the exchange reaction. This is surprising in that one might intuitively expect carbon dioxide adsorption, especially if it were dissociative in nature, to be slower than the carbon monoxide adsorption.

For example, Cha and Parravano (7) concluded that the rate limiting step in the titanium dioxide catalyzed oxygen exchange reaction was the carbon dioxide adsorption step. Furthermore, their calculations indicated that the subsequent dissociative breakdown of the adsorbed carbon dioxide was much faster than the molecular adsorption step.

That more than one type of adsorption for both carbon oxides is required to explain the data is not surprising. In Section I.2 it was stated that infrared studies (1, 51) indicated more than one type of carbon monoxide adsorption on zinc oxide. The added presence of more than one form of copper (54) on the surface of this catalyst leads to the conclusion that the surface is quite heterogeneous.

As was previously stated, this study was unable to determine whether the surface reaction proceeded via direct oxygen transfer or dissociative carbon dioxide adsorption. It can, however, be emphasized that the literature favors the copper as the active portion of the catalyst with respect to the exchange reaction. Two sources, Winter (56)

and Nekipelov and Kasatkina (39), stated that the exchange reaction was negligible over zinc oxide. In the latter paper it was further argued that dissociative carbon dioxide adsorption did not occur on zinc oxide. Stroeva et al. (48), however, did observe this reaction to be catalyzed by copper. Their results also indicated that the copper existed primarily in the metallic state. The nature of carbon dioxide adsorption on copper at this temperature is still open to question, however. Hayward and Gomer (23), for instance, found both associative and dissociative carbon dioxide adsorption on tungsten, and the same situation may well exist for copper.

A salient feature which was not noticed until the simulation studies were carried out is that for mixtures 1, 2, 4, and 7, the carbon dioxide G\* values increase linearly with respect to  $\ln t_r$  at sufficiently large values of  $t_r$ . This property could not be explained by one rate process alone because of the large range of  $t_r$  involved. Attempts to do this resulted in a serpentine approximation of the straight line. An attempt to describe this feature by two successive rate processes, steps 2 and 5, was still unsuccessful, as evidenced by the dashed curve in Figure IV-1. However, a series of three rate processes, or transformations during which additional steps become appreciable,

gives a much better approximation of this apparently linear relationship.

Figure IV-1 is a good example of this finding. very low  $t_{r}$  values,  $G^*$  for the carbon dioxide tracer is due to step 3 alone, with the subsequent surface reaction step and the slow carbon dioxide adsorption step both too slow to contribute to the observed response. As t increases the surface reaction of the adsorbed carbon dioxide begins to become important. This increases the amount of adsorption, and consequently G\* begins to increase. exchange reaction is not yet at equilibrium, however, because the carbon monoxide adsorption in step 2 is still negligibly slow. Just as this change in G\* has passed the inflection point and has begun to start leveling out, another process becomes important. This process is the approach to the equilibrium reaction provided by steps 2, 3, and 4. Using the equilibrium values for steps 1 through 4, equation (II-42) predicts the new value of G\*, which in this case is larger than that provided by carbon dioxide adsorption alone. Finally, after this process has nearly reached equilibrium, a third process begins to become important. Step 5, the slow carbon dioxide adsorption step. contributes to the last stage of the increase in G\*. Presumably, if there are no unaccounted for adsorption steps, G\* would finally level off at a value predicted by equation (II-35).

The greatest difficulties in fitting the data arose in mixtures 4 and 7, which are both almost pure carbon dioxide. In both cases carbon monoxide tracer was rapidly converted to carbon dioxide. Numerically it was not possible to obtain this degree of conversion without jeopardizing the carbon dioxide fit. This may suggest that under these conditions, in which the surface may contain a significant amount of oxygen, a competing step leading to the exchange reaction exists. Although there is no direct supporting evidence, a possible parallel mechanism might be

$$\begin{array}{c} 0 \\ \text{C0} + \overset{!}{\text{S}} \stackrel{?}{\leftarrow} \text{C0}_2 + \text{S} \end{array}$$

Another source of error is the extreme sensitivity of the numerical simulation to carrier gas composition when the mole fraction of one of the components nears zero. The analysis of mixture 4 was not very accurate because of the minimal amount of carbon monoxide present. Also, mixture 7 was classified as being 100% carbon dioxide, although the impurities may be as high as 0.5% as stated in Appendix B. Since one of the major impurities is carbon monoxide, the minimal differences between the data in Figures IV-4 and IV-7 are not surprising. It should also be added that explanation of the carbon dioxide data in Figure IV-7

required the presence of a small amount of carbon monoxide. Otherwise the linear variation of the carbon dioxide data discussed previously could not be simulated.

## IV.1.3 Equilibrium Regions

After the numerical simulations were carried out, it became easier to locate the plateaus in G\* where the analytical solutions of the theory presented in Sections II.4.1 and II.4.3 were valid. The following is a summary of regions in the various figures where these solutions hold:

Figure IV-1: At very low  $t_r$  values,  $G^*$  for the carbon dioxide data is approximately constant. This can be explained by assuming that step 3 is near equilibrium while the surface reaction step (step 4) is negligible. This situation is expressed by equation (II-41).

$$G^* = \mu_{C0}^{B'} \tag{II-41}$$

Figure IV-2: These results are similar to those in Figure IV-1. In addition, at low  $t_r$  values carbon monoxide adsorption is due only to step 1 and can be described by equation (II-40).

$$G^* = \mu_{C0}^{A^{\dagger}} \tag{II-40}$$

Figure IV-3: The low  $t_r$  behavior of both carbon monoxide and carbon dioxide can be explained as in Figure IV-2. In this case, however, a new plateau becomes evident in which the reaction is at equilibrium and the slow carbon dioxide adsorption step is still negligible. The region is defined roughly by 10 <  $t_r$  < 50 seconds. The value of G\* is predicted by equation (II-42). Using the values for the equilibrium constants that were found while fitting the data, the predicted value of G\* is 2.69 x  $10^{-5}$ , which is to be compared with the experimental value of approximately 2.7 x  $10^{-5}$ .

$$G^* = y_{C0}^s \mu_{C0}^t + y_{C0}^s \mu_{C0}^B^t$$
 (II-42)

Figure IV-4: This case is the same as Figure IV-1.

Figure IV-5: Carbon monoxide adsorption in a  $t_r$  range of 1 <  $t_r$  < 100 seconds can be described by equation (II-40).

Figure IV-6: This case is the same as Figure IV-5.

Figure IV-7: This case is the same as Figure IV-1.

# IV.2 Carbon Dioxide - Helium System

# IV.2.1 Basis for Experiments

The oxygen exchange reaction can conceivably occur

through either an associative carbon dioxide adsorption step with subsequent oxygen transfer to an adjacent carbon monoxide species, or a dissociative mechanism, in which surface oxygen and carbon monoxide species are formed. This latter step is represented by steps 3 and 4 in Section II.4.2. In the past chromatography has been used to distinguish between various types of adsorption. The theory presented in Appendix A can be applied to carbon dioxide if it is assumed that any carbon monoxide formed on the surface does not desorb as such. This assumption was verified in Section IV.1.2, in which simulation studies indicated that the desorption of carbon monoxide was indeed very slow. It is therefore desirable to distinguish between the two following carbon dioxide adsorption mechanisms:

$$C0_2 + S \stackrel{?}{\leftarrow} S$$
 (associative)

Indication that dissociative carbon dioxide adsorption might occur on this catalyst was obtained from the experiment discussed in Section IV.1. In Figure IV-8 plots of  $\ln G^*$  as a function of  $t_r$  are shown for the two carrier gases with the minimum carbon dioxide to carbon monoxide

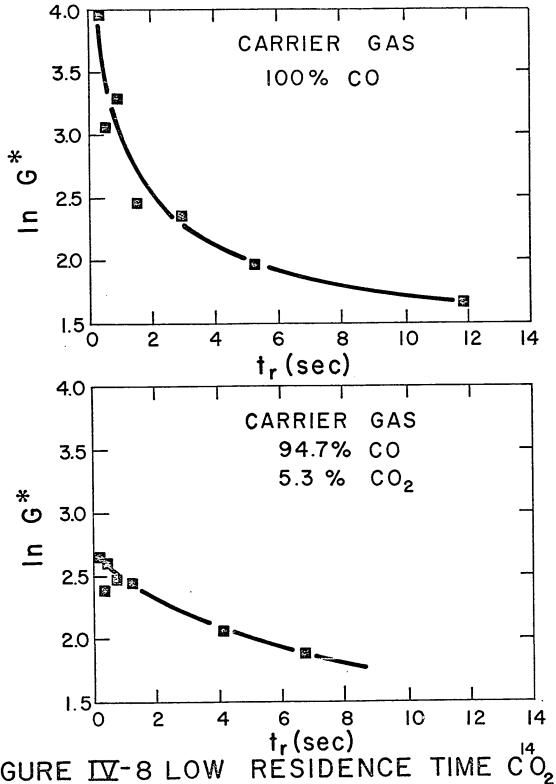


FIGURE IV-8 LOW RESIDENCE TIME CO DATA IN RICH CO CARRIER GASES

ratio. These results show that as  $y_{\text{CO}_2}$  becomes small, the limiting value of G\*, as  $t_r$  approaches zero, becomes very large. Furthermore, G\* at low  $t_r$  values is due primarily to adsorption and not reaction. According to equation (A-6), this type of behavior is to be expected when dissociative Langmuir adsorption is present. Data for carbon monoxide samples in rich carbon dioxide carrier gases, shown in Figure IV-9, can be seen to contrast this type of behavior. In this case the limiting values of  $\ln$  G\* do not seem to increase in the same manner as the data in Figure IV-8.

# IV.2.2 Experimental Results

It was decided therefore to conduct a brief investigation of the carbon dioxide - helium system. The raw data and calculated results for the six carrier gases used are shown in Appendices G and H, respectively. The same flow rate was used in all cases, and, as with the carbon monoxide-carbon dioxide system, all work was carried out at 400°F and atmospheric pressure. The experiments were abbreviated for two reasons. First, since the simulation work had not yet been completed by the time these experiments were conducted, it was not known whether or not the dissociative theory could be applied. Second, the absence of carbon monoxide in the carrier gas might tend to leave most of the

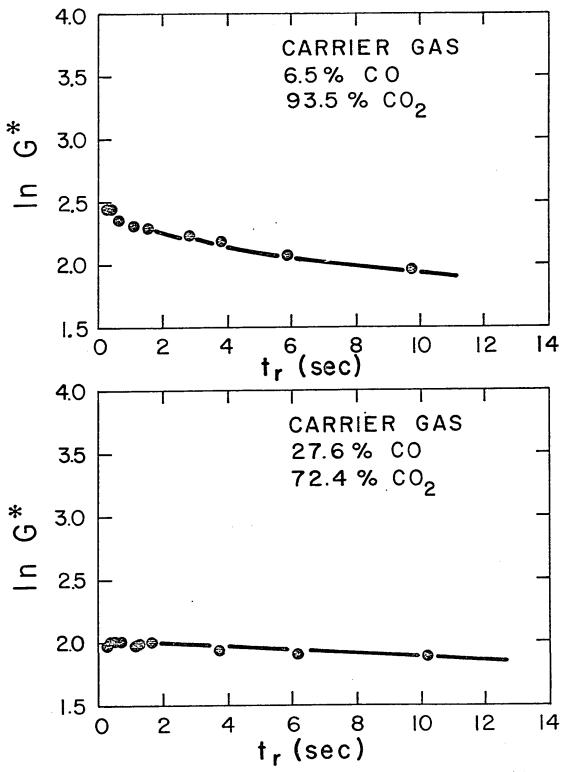


FIGURE IV-9 LOW RESIDENCE TIME C<sup>14</sup>O

DATA IN RICH CO<sub>2</sub> CARRIER

GASES

sites oxygenated if dissociative adsorption did occur.

The resulting surface, then, might be very much unlike the one over which the experiments with the carbon monoxide - carbon dioxide system were completed.

The results shown in Appendix H show that G\* increases as  $y_{\text{CO}_2}$  approaches zero. If Langmuir two site adsorption exists equation (A-7) should be valid, and the product G\*  $y_{\text{CO}_2}^{1/2}$  should approach a constant as  $y_{\text{CO}_2}^{}$  approaches zero. In Figure IV-10 the data are plotted in this form. It is quite apparent that this relationship does not hold.

At this point it was decided to check for Freundlich behavior. The form of G\* for a Freundlich isotherm is presented in Appendix A. A plot of  $\ln$  G\* versus  $\ln$  y<sub>CO2</sub>, which is indicated by equation (A-10), is shown in Figure IV-11. The resulting straight line demonstrates that a Freundlich isotherm does explain the data. The value of the constant d in this case is -0.84. The Freundlich isotherm can be derived by assuming that the heat of adsorption varies exponentially with surface coverage. Consequently, the assumption of a constant heat of adsorption, as required by the Langmuir model, has been demonstrated to be invalid.

#### IV.3 Conclusions

Chromatography and, more specifically, the use of

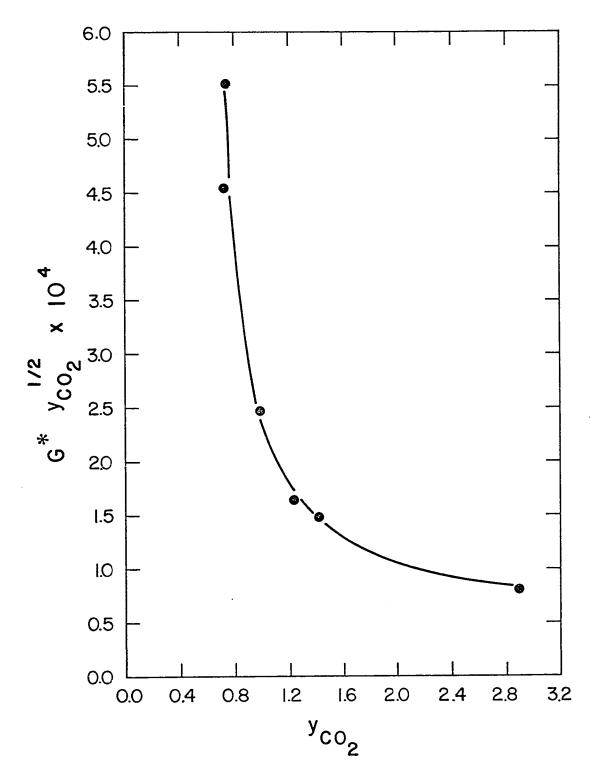


FIGURE IV-10 LANGMUIR TWO SITE ADSORPTION TEST FOR CO2

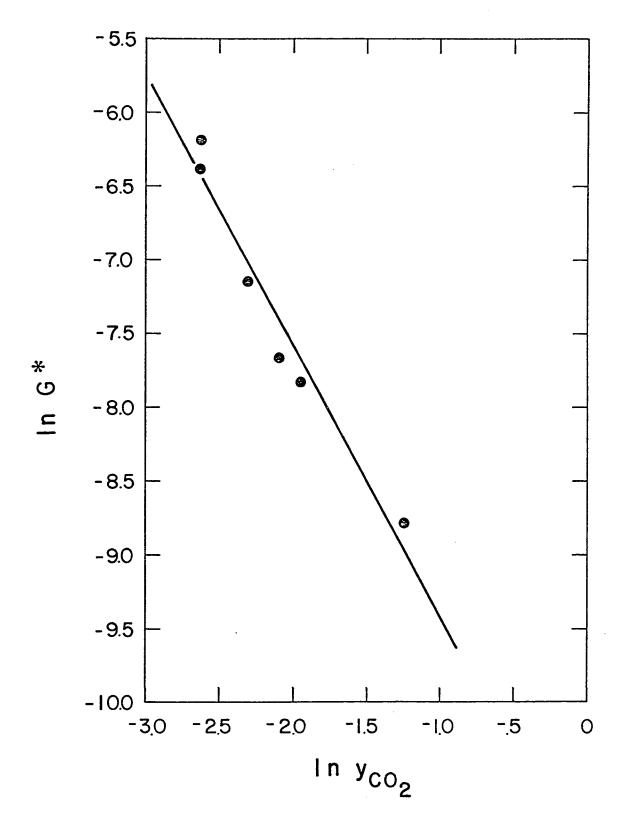


FIGURE IV-II FREUNDLICH TEST FOR CO2 - HE SYSTEM

isotopic tracers have once again been demonstrated to be an effective tool for investigating adsorption phenomena. In this case, the extension to cases involving nonequilibrium reactions has resulted in a somewhat more difficult theoretical problem. Several conclusions have been reached, however, by this method regarding the carbon monoxide - carbon dioxide system in the presence of a copper - zinc oxide catalyst at 400°F.

- 1. Based on the mechanism used to explain the data, there are at least two types of carbon monoxide adsorption on this catalyst. One form is rather rapid while the other is considerably slower. The slower form is involved in the oxygen exchange reaction.
- 2. Similarly there are two types of carbon dioxide adsorption, but in this case the faster process leads to the exchange reaction.
- 3. The rate limiting step in the exchange reaction has been found to be a carbon monoxide adsorption step.
- 4. The surface of this catalyst has been found to be energetically heterogeneous. This is indicated by the inability to fit a Langmuir model to the data and by the Freundlich nature of the carbon dioxide adsorption.
- 5. Attempts to distinguish between associative and dissociative carbon dioxide adsorption have been inconclusive.

6. The effect of varying the carrier gas flow rate has been demonstrated an important one. This result casts some doubt on the reliability of chromatographically determined isotherms on surfaces where nonequilibrium processes may be present despite being assumed nonexistant.

#### APPENDIX A

## THEORETICAL DETAILS

### A.1 Associative Adsorption

Consider a gas which only adsorbs molecularly on the surface of the catalyst. The Langmuir equilibrium relation takes the following form:

$$n_{i}^{\prime} = \frac{a y_{i}}{1 + b y_{i}} \tag{A-1}$$

where: a, b are constants at a given temperature

When expressed in the form of equation (II-16), the equilibrium function  $\mu_{\bf i}^{\prime}$  becomes

$$\mu_{i}' = \frac{a}{1+b y_{i}} \tag{A-2}$$

For the case described in Sections II.2.2 and II.4.1, in which no chemical reaction exists, it was shown that  $\mu_i^!$  was equal to G\*. In the limit, as  $y_i$  becomes very small, G\* approaches a constant, a.

$$\lim_{i} G^* = a$$

$$y_i \to 0$$
(A-3)

## A.2 Dissociative Adsorption

Consider the alternative to Appendix A.1 in which the gas is diatomic and dissociates upon adsorption. The Langmuir equilibrium relation becomes

$$n_{i}' = \frac{a y_{i}^{1/2}}{1 + b y_{i}^{1/2}}$$
 (A-4)

When expressed in the form of equation (II-16), the equilibrium function  $\mu_{\, {\bf i}}^{\, {\bf i}}$  becomes

$$\mu_{i}^{!} = \frac{a y_{i}^{-1/2}}{1 + b y_{i}^{1/2}}$$
 (A-5)

For the conditions referred to in Appendix A.1, G\* was shown to be equal to  $\mu_i^*$ . Therefore, in the limit as  $y_i$  approaches zero, G\* approaches infinity; that is,

$$\lim_{i \to 0} G^* = ay_i^{-1/2}$$

$$y_i \to 0$$
(A-6)

If  $G^*$  is multiplied by  $y_i^{1/2}$ , the following limiting expression is obtained:

$$\lim_{i \to 0} G^* y_i^{1/2} = a$$
 (A-7)

# A.3 Freundlich Adsorption

A third type of adsorption isotherm is the Freundlich type. The Freundlich relationship is

$$n_i' = fy_i^d$$
 (A-8)

where: f, d = constants at a given temperature.

When expressed in the form of equation (II-16), the equilibrium function  $\mu_1^{\prime}$  becomes

$$\mu_{i}^{!} = fy_{i}^{d-1} \tag{A-9}$$

For the case described in Appendix A.1,  $G^*$  was shown to be equal to  $\mu_1^!$ . Therefore  $G^*$  becomes

$$G^* = fy_i^{d-1} \tag{A-10}$$

A.4 Relationship Between  $\mu_{C0}^{B}$ ,  $\mu_{C0}^{B}$ , and  $K_{4}^{*}$ 

The fact that only two of the above equilibrium constants are independent can be easily shown. Since

$$K_{4}^{\prime} = \frac{n_{C0}^{B}}{n_{C0}^{B}}$$
 (II-38d)

and

$$\mu_{C0}^{B} = \frac{n_{C0}^{B}}{y_{C0}}$$
 (II-38b)

$$\mu_{C0_{2}}^{B} = \frac{n_{C0_{2}}^{B}}{y_{C0_{2}}}$$
 (II-38c)

it follows that

$$K_{4}' = \frac{{}^{\mu}_{C0}^{B} y_{C0}}{{}^{\mu}_{C0}_{2} y_{C0}_{2}}$$
 (A-11)

where the ratio  $\frac{y_{C0}}{y_{C0}_2}$  was shown in Section II.2.3 to remain constant for a given carrier gas in the vicinity of the tracer.

#### APPENDIX B

#### **MATERIALS**

## B.1 Helium, Argon

Helium and argon were both purchased in 1A cylinders. The helium was supplied by Iweco and had a stated minimum purity of 99.99%. The Matheson Company supplied the argon, which had a minimum purity of 99.995%.

#### B.2 Hydrogen

Hydrogen was purchased from the Matheson Company in a 1A cylinder. The Ultra High Purity grade had a purity of 99.999%.

#### B.3 Carbon Monoxide, Carbon Dioxide

Both carbon oxides were purchased from the Matheson Company in 1A cylinders at 99.5% minimum purity.

#### B.4 Radioactive Gases

The radioactive tracers were obtained from the New England Nuclear Company. Two millicuries of each, or a

total of four millicuries, were used throughout this work. The gases were shipped in glass ampoules containing one millicurie each. In the first shipment the specific activities of the carbon dioxide and the carbon monoxide were 30.8 and 4.5 millicuries per millimole, respectively. In the second shipment these respective values were 20.0 and 4.5.

### B.5 Catalyst

The catalyst under study was Girdler G-66B Low Temperature CO Conversion catalyst, manufactured by the Catalysts Division of the Chemetron Corporation. The unreduced catalyst, consisting of copper oxide supported on zinc oxide, was received in the form of 1/4" x 1/8" pellets courtesy of Mr. Luis Guzman of Chemetron. The manufacturer listed the BET surface area as 25.4 m<sup>2</sup>/g and Suzuki and Smith (49) experimentally determined it to be 35.9 m<sup>2</sup>/g. These authors have presented a table of physical properties of this catalyst in both the unreduced and the reduced states based on their own investigation.

#### APPENDIX C

#### EXPERIMENTAL APPARATUS

#### C.1 Equipment Layout

The oven, temperature controller and heat source were all purchased in one integrated unit which stood approximately five feet high. A large metal stand was used to support the recorder, the electrometer, the thermal conductivity bridge and the D.C. power supply. Between the instrument stand and the oven was a large frame-like support constructed of slotted angle iron. Wooden shelves were placed in portions of this structure in order to support the preamplifier and the vacuum pump. The remainder of the equipment was mounted on the angle iron structure. The gas cylinders were clamped to this center support.

# C.2 Tubing, Valves, Filters, Fittings

In general 1/8" type T Polypenco Nylaflow tubing was used. The primary advantage offered by this tubing was the ease of handling because of its flexibility and easy cutting. Because of the temperatures involved, stainless steel tubing was used to connect with the columns in the

oven. The sampling valve, test column, thermal conductivity cell and ionization chamber were connected by 1/8" x .042" stainless steel tubing. This size was selected in order to minimize dead volume in this region. The precolumn connecting tubing was also 1/8", but the wall thickness was .035" instead. The 1/16" tubing used in the construction of the bypass and the pressure taps is described elsewhere.

Swagelock fittings were used exclusively. Nearly all fittings were brass, although stainless steel was used on occasion.

Whitey OKS2 or ORS2 forged body valves were used almost exclusively. Exceptions were the two Whitey OGS2 toggle valves, a Whitey OKM2-S2A forged body valve used for tracer supply cutoff, and the metering valves.

#### C.3 Flow Control and Measurement

Flow control was provided by a constant differential type flow controller manufactured by the Moore Products Company. The specific model, 63BU-L, was constructed of brass and designed for low flow rates with a constant upstream pressure. The controller provided a constant pressure differential across a stainless steel Nupro very fine metering valve. Flow was varied by adjusting the metering valve.

Flow rates were measured by timing the displacement of soap bubbles in a 50 cc soap bubble meter. The timing device used was manufactured by the Precision Scientific Company and recorded time in tenths of a second.

# C.4 Temperature Control and Measurement

The precolumn and the test column were thermostated in a Con-Wate Ultra-Temp oven, manufactured by the Blue-M Electric Company. Control to within 0.4°F was obtained over the short range, but over a period of days the temperature was observed to vary over a 5°F range. A temperature guard system was installed on the oven in order to prevent a temperature runaway resulting from a temperature controller malfunction.

For temperature measurement a chromel alumel thermocouple was positioned in the oven. The output was measured on a Leeds and Northrup model 8686 millivolt potentiometer.

In all, then, there were three thermocouples in this oven. One was for temperature control; another for temperature measurement; and the third for the runaway guard system.

#### C.5 Pressure Measurement

Pressure taps were installed inside the oven so that

once again stainless steel connecting tubing was employed. In keeping with the objective of minimizing dead volume, additional fittings were not incorporated for these pressure taps. Instead, 1/16" holes were tapped in the unions at the ends of both the short and the long columns (3 unions, since the columns were joined together), and lengths of 1/16" x .010" stainless steel tubing were silver soldered into place. Reducing unions (1/16" x 1/8") joined the 1/16" tubing to 1/8" tubing, which led directly to the three pressure gages. These Crosby gages measured pressures from 30" Hg vacuum to 15, 30 and 60 psig, respectively. Only two of these gages were really necessary. Therefore, the 60 psig gage was used only as a check on the other two gages.

#### C.6 Test Column and Precolumn

The precolumn was installed upstream of the test column in an attempt to remove any poisons in the carrier gas before reaching the test column. A 61.2 cm length of 3/8" x .035" stainless steel tubing was used to contain 39.3684 g of catalyst which had been ground and seived to a 35/48 Tyler mesh particle size range. Both ends of the column were fitted with glass wool plugs in order to hold the bed in place. A Mettler balance was used in all catalyst weighings.

The test column consisted of a long and a short column in series. As described previously, it was possible to use either the short column alone, or the two columns in series for experiments. Both columns were constructed of  $1/4" \times .035"$  stainless steel tubing. The short column contained 2.2671 g of 28/35 Tyler mesh catalyst and had a length of 10.0 cm. The long column was 101.4 cm long and contained 26.0905 g of 28/35 mesh catalyst. As with the precolumn, glass wool plugs were inserted in both columns. The two columns were connected by a 1/4" Swagelock union and wound into a helix. Two 1/16" holes were tapped in the side of this fitting in order to accomodate two lengths of 1/16" x .010" stainless steel tubing. These connections were silver soldered into place. One of these was a pressure tap, while the other was available to direct the carrier gas over the short column only when so desired. At the ends of the resulting test column Swagelock fittings were similarly tapped. As with the center fitting, one tap in each fitting was constructed for pressure measurement. A 2 1/2" section of 1/16" x .028" stainless steel capillary tubing was silver soldered into the remaining two holes in order to provide a partial bypass flow when the columns were operated in the combined mode. Proper proportioning of the flow between the bypass and the column could not be obtained a priori by selection of the appropriate inside

diameter. Therefore, it was necessary to flatten the bypass very slightly with a hammer until the desired bypass to column ratio could be approximated. Determination of the fraction of flow through the bypass is discussed in Appendix D.

A third 1/16" tap was provided at the short column exit. The 1/16" x .010" section of tubing, which was silver soldered in place, was connected to 1/8" x .042" tubing. This line was connected to one of the toggle valves and was used to generate a bypass peak when operating with the short column.

## C.7 Sample System

The sample system is shown in Figure III-3. It consisted basically of a sample loop, sampling valve, pressure gage, vacuum source, tracer supply and connection tubing. The sampling valve was a standard two position six way chromatographic sampling valve. The sample loop had a volume of approximately 0.29 cc.

The stainless steel tubing in the manifold was 1/8" x .042", as every effort was made to minimize the dead volume and thus conserve the radioactive tracer. The pressure gage, manufactured by the Marsh Instrument Company, measured pressure from 30" Hg vacuum to 250 psig.

The system was designed so that not all the radioactive tracer would have to be diluted simultaneously. High vacuum stopcocks were joined to the glass ampoules in which the tracers were shipped while the breakseals remained un-Kovar seals were joined to the other sides of the stopcocks in order to connect the assemblies to the Whitey valves, which in turn were connected to the manifold by Swagelock fittings. The space between the valve and the stopcock provided an excellent dilution volume, into which a portion of the tracer could be expanded and then diluted by the carrier gas, if necessary. In addition to these mixing volumes, a 30 cc Hoke 4HS30 sample cylinder was connected to the manifold. This container was used to hold some of the radioactive carbon monoxide which had been diluted with mixture 1.

It was felt that by employing the high vacuum stopcocks and the original glass ampoules better protection against air contamination could be achieved than by methods used by previous investigators.

# C.8 Thermal Conductivity System

The thermal conductivity cell was used to measure concentration disturbances in the gas exiting the column.

In free volume determinations argon peaks were monitored

as the helium carrier gas swept the sample through the cell. In experiments involving the carbon oxide mixtures as carrier gases, the thermal conductivity system was used to determine if the chromatographic system was at equilibrium before a sample was injected. Concentration peaks were not used in chemisorption analysis because of small amplitude and variable polarity.

The thermal conductivity system is shown in Figure C-1. The cell was a Gow-Mac model 133 micro-thermal conductivity cell. It was constructed of stainless steel and had an internal volume of 0.115 cc. Detection was provided by a matched pair of 8K ohm glass bead thermistors mounted inside the cell. The response time was stated by the manufacturer to be less than 0.5 second. The assembly was mounted on a wood support and no attempt was made to insulate the cell from ambient conditions.

The thermistors were an integral part of a standard wheatstone bridge assembly, which in this case was a homemade device. The D.C. power supply was a Kepco model ABC 75-2. The device was set at 7.5 volts throughout this study, and bridge currents of approximately 3 milliamperes were typical. The bridge output was connected to the recorder channel which was equipped with the integrator.

# Numerical Legend Figure C-1

- 1. D.C. Power Supply
- 2. Bridge Assembly
- 3. Recorder
- 4. Thermistor Mounting
- 5. Thermal Conductivity Cell
- 6. Flow From Precolumn
- 7. Flow From Test Column

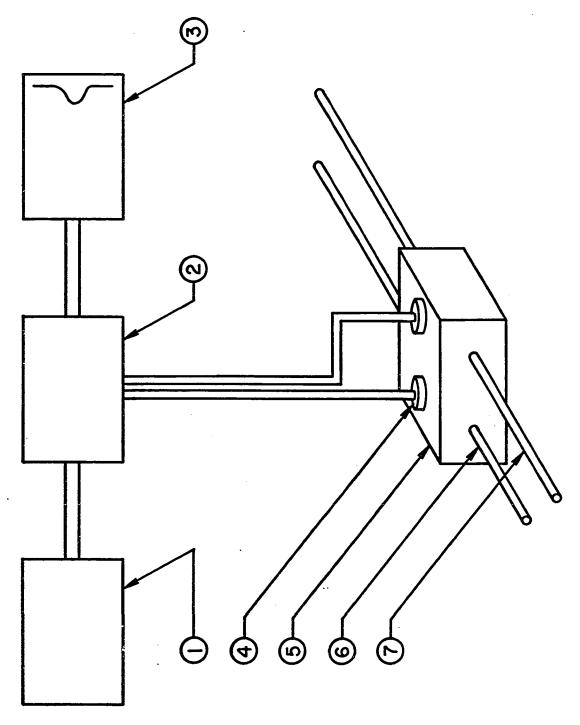


FIGURE C-I THERMAL CONDUCTIVITY DETECTION SYSTEM

#### C.9 Radioactive Detection System

The eluted radioactive sample was detected in a 3 cc stainless steel ionization chamber. Figure C-2 shows the chamber, along with a schematic diagram of the radioactive detection system. The chamber was designed specifically for this type of service and had been used previously by other investigators. The outer wall of the chamber served as one electrode, while a 1/8" polished stainless steel rod in the center of the chamber served as the other. A six volt potential, supplied by four 1.5 volt Burgess dry cells connected in series, was placed across these electrodes. The center electrode was insulated from the chamber by Kel-F. Care had to be taken to insure that this Kel-F spacer re-On several occasions water and fine catalyst mained clean. particles contaminated the insulator during the activation process. Inability to zero the electrometer resulted.

As the radioactive molecules enter the detector, the energy released during the decay process ionizes some of the surrounding gas molecules. The ions are caught in the resulting field and migrate to the appropriate electrodes. A small current, which is proportional to the level of radioactivity in the chamber, results. Currents of the order of  $10^{-14}$  amperes were typical in this work. The preamplifier was connected to the Model 401 Cary Vibrating

# Numerical Legend Figure C-2

- 1. 1/8" Nylon Tubing
- 2. S S Connector
- 3. Ionization Chamber
- 4. Preamplifier
- 5. Electrometer
- 6. Recorder
- 7. 6 Volt Dry Cell
- 8. S S
- 9. Ke1-F
- 10. Brass
- 11. Brass Adapter
- 12. Teflon

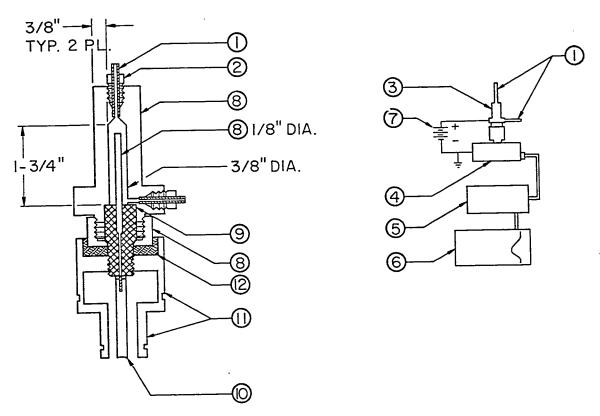


FIGURE C-2 RADIOACTIVE DETECTION SYSTEM

Reed Electrometer by a four foot coaxial cable. The electrometer was operated with the resistor set at  $10^{12}$  ohms. The preamplifier was in the critical damping mode. The output of the electrometer was fed to the recorder for simultaneous monitoring with the thermal conductivity output. Operation in the critical damping mode resulted in a response time of approximately 1 second.

### C.10 Recorder

Both the thermal conductivity cell and the ionization chamber responses were recorded on a Hewlett-Packard Model 7100B two channel recorder. One channel, the thermal conductivity channel, was provided with an integrator. The instrument was capable of measuring voltages varying from 1 millivolt to 100 volts. The chart speed could be varied from 1 inch per hour to 2 inches per second.

## C.11 Vacuum Pump

A Welch Duo-Seal vacuum pump was used to evacuate the sample manifold and portions of the flow system. Normally a 29" Hg vacuum was obtained.

#### APPENDIX D

### EXPERIMENTAL PROCEDURE DETAILS

## D.1 Catalyst Preparation and Activation

The catalyst was ground and sieved to 28/35 and 35/48 Tyler mesh fractions. The smaller particle size was used in the precolumn. The tubing was cut to the appropriate length, washed with acetone, and dried in a stream of nitrogen. A 1/8"-1/4" glass wool plug was placed in one The tubing was then secured by a clamp on a ringstand and held in a verticle position. Catalyst from a preweighed vial was then poured into the column through a funnel until the level rose to within 1/4" of the top. All the while the column was vigorously tapped in order to maximize pack-The top end was plugged with glass wool before installation in the oven. The vial was then reweighed and the weight of the catalyst in the column determined by differ-All three columns were prepared in this manner. The precolumn was installed and the long and short columns were connected in the series configuration.

The activation procedure was essentially the same as those used by Musser (38) and recommended by the

manufacturer. The helium flow rate was first established at approximately 3.7 cc/sec, ambient conditions. Hydrogen flow was then combined with the helium flow at such a rate as to result in a 1% hydrogen mixture. Simultaneously the oven was set at 400°F. Condensation could be observed in the exit lines shortly thereafter, indicating that reduction was taking place. After six hours the hydrogen flow was increased to give a 2% mixture. After a second six hour period the hydrogen level was increased to 5%. At the end of the final six hour period the flow of hydrogen was terminated, and the helium flow was reduced in preparation for the free volume and bypass calibration procedures. It was necessary to know, of course, the proper hydrogen metering valve settings before activation was started.

The activation step apparently was reproducible from one column to another. In some preliminary work which led to the work described in this thesis, a different column was prepared and activated by the same procedure described above. Adsorption data with mixture 1 gave results which were identical, within experimental error, to results from columns discussed herein.

A check on the catalyst activity with respect to time was accomplished by comparing the level of adsorption with a mixture 1 carrier gas at a given flow rate. The first check was carried out upon the completion of experiments with mixtures 1, 2 and 3. It showed only slight, if any, deactivation. After work with mixtures 4, 5 and 6 was finished, a second check was made. In this case the activity had decreased to approximately 84% of the original level. After mixture 7 experiments were completed, a final check showed that about 17% of the activity had been lost. These check points are shown in Figure IV-1.

#### D.2 Carrier Gas Mixtures

A mixing manifold was constructed to facilitate preparation of the carrier gas mixtures. The valves were Whitey OKS4 stainless steel forged body valves. The connecting tubing was 1/4" x .035" stainless steel. A Heise 0-1000 psia gage was used to measure the pressure as the gases were expanded into a previously evacuated 1A gas cylinder. The mixing cylinder was actually purged with one of the carbon oxides and evacuated three times. Each gas was slowly expanded from its supply into the mixing cylinder until the desired pressure was attained.

Final composition analysis of the carbon monoxidecarbon dioxide mixtures was made on a Consolidated Electrodynamics Type 21-104 mass spectrometer. Carbon dioxidehelium mixture compositions were determined by pressure measurements before and after freezing the carbon dioxide in a vacuum system. The mixtures used in this work, along with their compositions are listed in Table D-1.

 $\underline{\text{TABLE D-1}}$  Carrier Gas Compositions

Mixture	Vol. % He	Vol. % CO <sub>2</sub>	Vol. % CO
1	0.0	93.5	6.5
2	0.0	72.4	27.6
3	0.0	36.5	63.5
4	0.0	99.6	0.4
5	0.0	5.3	94.7
6	0.0	0.0	100.0
7	0.0	100.0	0.0
8	92.7	7.3	0.0
9	71.1	28.9	0.0
10	85.8	14.2	0.0
11	90.0	10.0	0.0
12	92.8	7.2	0.0
13	87.6	12.4	0.0

# D.3 Radioactive Sample Preparation

A physical description of the sample manifold is presented in Appendix C. When the stopcock was joined to

the ampoule containing the tracer, a ball bearing was placed in a specially prepared pocket. The ball bearing was therefore held above and slightly to the side of the breakseal. The valves and the stopcock were positioned in such a way as to evacuate the sample manifold up to the breakseal. When the vacuum was deemed satisfactory, the stopcock was closed. A magnet was used to dislodge the ball bearing and cause it to fall on the breakseal. Several attempts were required because of the short distance of fall and the light weight of the ball bearing. When the seal was broken, the tracer was ready for use. Both tracer supplies were prepared for use in this manner.

A large amount of carbon monoxide tracer was expanded into the 30 cc sample container. The tracer in this container was then diluted by the addition of mixture 1. From these supplies samples could be diluted and expanded as necessary for injection.

#### D.4 Free Volume Calibration

For both the long and short columns free volume calibrations were made in order to determine the void volumes of the columns. From the free volume and the flow data, the carrier gas residence time,  $t_r$ , in the column could be calculated. The free volume,  $V_G$ , can be expressed

$$V_{G} = Q t_{r}$$
 (D-1)

Experimentally this determination was accomplished by injecting argon samples into a helium carrier stream. Argon, of course, does not adsorb and therefore travels through the column at the same velocity as the carrier gas. For the short column, two samples were required in order to determine a value for  $t_r$ . This procedure is described under Section III.2. For the long column, only one sample was required since one sample resulted in bypass and main column peaks. After correcting the measured flow rates to column conditions to obtain Q,  $V_G$  could be determined by equation (D-1).

For the short column the average free volume,  $V_{\rm G}$ , was 1.86 cc. The value of  $V_{\rm G}$  for the long column was 16.8 cc. The data and calculated results for these determinations are presented in Appendices G and H, respectively.

# D.5 Bypass Line Calibration

When the bypass was used it was necessary to know what portion of the flow approaching the column was diverted by the column. This was determined at the same time the free volume calibration was carried out. Since the thermal conductivity cell output was connected to the recorder

channel with the integrator, the areas of the peaks were known. The fraction of flow bypassing the column could be calculated by the following expression:

$$f_B = \frac{\text{area of bypass peak}}{\text{area of bypass peak} + \text{area of main peak}}$$

It was assumed that the thermal conductivity cell response was proportional to the argon concentration. This assumption was verified experimentally for the range of argon concentrations used.

When the columns were in series, 22.9% of the flow bypassed the column. As with free volume determinations results from a number of runs were averaged. The experimental  $\mathbf{f}_B$  values are included with the free volume data in Appendix G.

### D.6 Peak Analysis

The determination of the residence time of a sample in a column from a chromatogram can sometimes not be a straightforward task. Strictly speaking, graphical integration should be carried out in order to determine the centroid of the peak. In this work, however, this method was rendered useless because of the excessive tailing, which introduces large amounts of error into this procedure.

Selecting the peak maximum provided the easiest approach. This was totally satisfactory with the argon-helium data because of the smoothness of the peaks. However, with the radioactive peaks this method proved unreliable because of the stochastic nature of these peaks. The problem was finally resolved by the following procedure. A line was drawn through the peak parallel to the baseline at an amplitude equal to 50% of the maximum value. The segment of this line situated within the peak then was bisected. This point, then, represented the time reference point of the peak. The method showed good reproducibility. The data showed considerably less scatter when this method was used instead of attempting to locate the peak maximum.

### APPENDIX E

### SAMPLE CALCULATIONS

E.1 The average column pressure,  $P_c$ , was calculated for every run from the three pressure readings recorded as data.

$$P_{c} = \frac{P_{i} + P_{o}}{2} + P_{a}$$

$$P_{c} = \frac{(2.9 + 0.0)}{2} \text{ psig} \cdot 51.71 \frac{mm}{psig} + 30.520 \text{ in Hg} \cdot 25.4 \frac{mm}{in}$$

$$P_{c} = 852.8 \text{ mm Hg}$$

E.2 The column flow rate, Q, was calculated from the measured flow rate as follows:

$$Q = Q_{m} \cdot \frac{P_{a}}{P_{c}} \cdot \frac{T_{c}}{T_{r}} \cdot (1 - \frac{P_{H_{2}0}}{P_{a}}) \cdot (1 - f_{B})$$

$$Q = 1.0860 \frac{cc}{sec} \cdot \frac{775.2 \text{ mm}}{852.8 \text{ mm}} \cdot \frac{477.9 \text{ °K}}{296.3 \text{ °K}} \cdot (1 - \frac{21.196 \text{ mm}}{775.2 \text{ mm}}).$$

$$(1 - .229)$$

$$Q = 1.1943 \frac{cc}{sec}$$

For the short column,  $f_B = 0$ .

E.3 The column free gas volume,  ${\rm V}_{\rm G}$ , was calculated from the argon - helium data as follows:

$$V_G = Q \cdot t_r$$
, where  $t_r = t_p$  for argon.

$$V_{G} = 0.2331 \frac{cc}{sec} \cdot 72.0 sec$$

For the long column,  $\mathbf{V}_{\mathbf{G}}$  values for various runs were averaged.

$$V_{G} = \frac{(17.05+17.00+17.00+17.00+16.64+16.78+16.92+16.57+16.66+16.57)}{10}$$

$$V_G = 16.8 \text{ cc}$$

For the short column, one average residence time was determined for each of three flow rates with the corresponding  $V_{\rm G}$  values subsequently being calculated. These latter values were then averaged.

$$V_G = \frac{1.898 + 1.867 + 1.829}{3}$$

$$V_G = 1.86 \text{ cc}$$

E.4 The fraction of flow going through the bypass,  $f_{\rm B}$ , was calculated as follows from the argon - helium data:

$$f_B = \frac{A_B}{A_B + A_C}$$

$$f_B = \frac{1.36}{1.36 + 4.55}$$

$$f_{B} = 0.230$$

The individual determinations were then averaged.

$$f_{B} = \frac{.232+.230+.226+.223+.228+.231+.231+.228+.232+.229}{10}$$

$$f_{B} = 0.229$$

E.5 The residence time of the carrier gas flowing through the column,  $t_r$ , could then be calculated as follows:

$$t_{r} = \frac{V_{G}}{Q}$$

$$t_r = \frac{16.8 \text{ cc}}{1.194 \text{ cc/sec}}$$

$$t_r = 14.1 \text{ sec}$$

E.6 The peak residence times were calculated differently depending on which column was in use. For the long column the following procedure was followed:

$$t_{p} = L_{r} \cdot \frac{1}{C_{s}}$$

$$t_{p} = 2.15 \text{ in } \cdot \frac{1}{2 \text{ in/min}} \cdot 60 \text{ sec/min}$$

$$t_{p} = 64.5 \text{ sec}$$

The peak residence time in the short column was calculated as follows:

$$t_p = L_{r1} \cdot 1/C_{s1} - L_{r2} \cdot 1/C_{s2}$$
 $t_p = 4.43 \text{ in } \cdot 1/(2 \text{ in/sec}) - 2.16 \text{ in } \cdot 1/(2 \text{ in/sec})$ 
 $t_p = 1.14 \text{ sec}$ 

E.7 The column conversion constant,  $\beta$ , was calculated as follows:

$$\beta = \frac{m}{V_G c}, \text{ where } c = \frac{P_c}{R T_c}$$

$$c = 852.8 \text{ mm/}(62360 \frac{mm cc}{g \text{ mole} \text{ k}} \cdot 477.9 \text{ k})$$

$$c = 2.862 \cdot 10^{-5} \text{ g mole/cc}$$

$$\beta = \frac{28.3576 \text{ g catalyst}}{16.8 \text{ cc} \cdot 2.862 \cdot 10^{-5} \text{ g mole/cc}}$$

$$\beta = 5.899 \cdot 10^4 \text{ g catalyst/g mole}$$

E.8 G\* was then calculated according to the equation

$$G^* = \frac{1}{\beta} \cdot (t_p/t_r - 1)$$

$$G^* = \frac{1}{5.899 \cdot 10^4} \cdot (64.5/14.1 - 1)$$

$$G^* = 6.059 \cdot 10^{-5}$$
 g mole/g catalyst.

#### APPENDIX F

### ERROR ANALYSIS

## F.1 Temperature

A 0.2°C graduated mercury thermometer was used to measure the room temperature to within  $\pm$  0.1 °C. For a room temperature of 23°C, the error in  $T_r$  is  $\pm$  (0.1) (100)/296 =  $\pm$ 0.034%.

The short term fluctuation of the column temperature,  $T_c$ , was less than  $\pm 0.2$  °C. The resulting error in  $T_c$  is  $\pm (0.2)$  (100)/477 =  $\pm 0.042$ %.

### F.2 Pressure

The atmospheric pressure was measured to within  $\pm 0.005$  inches of mercury. The error in P<sub>a</sub> is  $\pm (.005)$  (100)/30 =  $\pm 0.017\%$ .

The inlet pressure was measured on a gage which could be read to an accuracy of  $\pm 0.05$  psi. For an inlet pressure of 2 psig the resulting error in P<sub>i</sub> is  $\pm (.05)(100)/16.7 = \pm 0.30\%$ .

The same degree of accuracy was obtained for the outlet pressure gage, and the resulting error in  $P_{\scriptscriptstyle O}$  for an

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outlet pressure of  $\pm 0.5$  psig is  $\pm (.05)(100/15.2 = \pm 0.33\%$ .

The average column pressure was calculated by the formula  $P_c = \frac{P_i + P_o}{2} + P_a$ . For an average pressure of 820 mm, the error in  $P_c$  is  $\pm ((.30 + .33)/2 + .017) = \pm 0.33\%$ .

## F.3 Time and Distance

Distance measurements on recorder charts were made to within  $\pm(.01)(100)/2 = \pm0.5\%$ .

A stopwatch graduated in tenths of a second was used to measure time elapsed in recording flow rates with the bubble meter. Repeated measurements were reproducible to within  $\pm 0.3$  sec for a 100 sec time interval. The resulting error in the measured flow rate,  $Q_{\rm m}$ , is  $\pm (0.3) (100)/100 = \pm 0.3\%$ .

### F.4 Column Flow Rate

The column flow rate is given by

$$Q = Q_{m} \cdot (P_{a}/P_{c}) \cdot T_{c}/T_{r}, \cdot (1 - \frac{P_{H_{2}0}}{P_{a}}) \cdot (1-f_{B}).$$

The resulting error in Q is  $\pm(.30 + .33 + .078 + .024 + .27) = \pm 1.0\%$ .

## F.5 Catalyst Weight

The catalyst was weighed on a Mettler balance to an accuracy of  $\pm 0.0001$  g. But due to the handling procedure in packing the columns it is doubtful that the weight of the catalyst, m, was known to limits better than  $\pm 0.001$  g. For the short column this results in an error of  $\pm (.001)$   $(100)/2.2671 = \pm 0.044\%$ .

For the long column the error in m is  $(.001)(100)/28.3576 = \pm 0.004$ %.

# F.6 Bypass Fraction

The peak areas,  $A_C$  and  $A_B$ , used in calculating the fraction of flow which bypassed the column could be determined to within  $\pm 0.01$ . For a typical determination, in which  $A_C$  = 4.55 and  $A_B$  = 1.36, the resulting error in  $f_B$  =  $\pm (.0021)(100)/0.230$  =  $\pm 0.91\%$ .

### F.7 Column Free Volume

The column free volume,  $V_G$ , was determined by the product Q ·  $t_p$ , where the  $t_p$  referred to the residence time of an argon sample in a helium carrier gas. The error in  $V_G$  is therefore =  $\pm(1.0 + 0.5) = \pm1.5\%$ .

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# F.8 Column Conversion Constant

The column conversion constant,  $\beta$ , was determined by the expression,  $\beta = \frac{m}{V_G c}$ . When the ideal gas law is assumed, this becomes  $\beta = \frac{mRT_c}{V_G P_c}$ . The error in this term then is =  $\pm (.044 + .042 + .33 + 1.5) = \pm 1.92\%$ .

## F.9 G\* Error

The resulting error in G\*, calculated by  $(1/\beta)$   $(t_p/t_r - 1)$ , is  $\pm (1.92 + 3.85) = \pm 5.77\%$ .

# APPENDIX G

RAW DATA

RAM DATA - MIXTURE 1

6.5 % CO 93.5 % CO2

T TIME, SEC	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
SAMPLE RET	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
POPPSIG	
PIAPSIG	mm NV 4 444 00 00 00 00 00 00 00 00 00 00 00
PA, IN HG	$\begin{array}{c} \mathbf{u}_{1}  \mathbf{u}_{2}  \mathbf{u}_{1}  \mathbf{u}_{2}  \mathbf{u}_{2}  \mathbf{u}_{3}  \mathbf{u}$
TC+DEG C	50 00 00 00 00 00 00 00 00 00 00 00 00 0
TR.DEG C	00 00 00 00 00 00 00 00 00 00 00 00 00
TOTAL FLOM RATE, CC/SEC	44 W W W W W W W W W W W W W W W W W W
COLUAN	S S S S S S S S S S S S S S S S S S S

RAM DATA - MIXTURE 2

27.6 % CO 72.4 % CO2

																																_	
RET TIME, SEC	1.19	-	_	-:	-:				_	. ~				4	_	7	10	2	1.8	10					8		000	96.8	01.6	20.00	7 4 . 0		0770
SAMPLE	0140	=	_	=	Ξ.	≕	3	Ξ	5	Ξ	7	. =	717	_ =	C 1 4	_	C 1 6	_	210	_	10		C14	0	C14		C14	4	_	C 1 4	_	C14	0
Pospsia	0 8 8		÷	-	÷	-		•=	_	-	_	_	~	_	_	_	_	_	0			. 0	_	_	0	0	0	0	C	0	0	0	0
PISPSIG	2.80	•	•	~	ĭ	~	Ξ	Ξ	~	~	ď	ď.		_		•	N	Č	~	N	-	-	Ò	0	0	0	0	0	0	•	•	~	~
PA. IN HG	30,090	5	•	•	•		•		-	-	Š	Š	7:0	ŏ:	. 15		9.08	9.0	60 •	600	. 15	. 15	. 22	. 22	:21	:21	• 00	, 21	151	• 18	• 18	. 13	. 13
TC.DEG C	203+3	2 0	Š	วัง	2 6	ກັ	m (	2	<u> </u>	ž	Ĕ	~	ž	Ĕ	ž	ň	ĕ	Ē	Ť	ř	ż	ě	Ę.	<u>ت</u>	÷	ŭ	3	ě	÷	ë	÷	ë.	÷
TR,DEG C	© © © ©	, .	•	•		ě 4	ĕ.	š			õ	~	~	<u>.</u>	•	-	<u>.</u>	-	•	_	•	•	•	-	•	•	•	•	•	•	•		•
TOTAL FLOW RATE,CC/SEC	4 . 5249 4 . 5249	# # # # # # # # # # # # # # # # # # #	0.00 to	2 × × × × × × × × × × × × × × × × × × ×	0000000	0000+7	75001	\0 \0 \0 \0	2000+1	1+0002	0.7326	0.7326	0.4324	0.4324	0.3200	00 3200	0.193	0.1936	0.1177	0.1177	0.0780	0.0780	1 0526	1 • 05.26	2	90	24	0.3236	23	52	3	0.0763	0
COLUMN	SHORT	SHORT	1000	TACH.	FOUND	10000	- XOC 7 0	- 2000	- 100	- HOLE	SHCRI	- HOLE	SHURT	SHURT	SHURI	L XOX	SHURT	SHURT	SHURT	SHURT	SHORT	SHURI	9 KO .	9 C S	S C C	P C C	5 × 0 × 0	520	5 NO.	SNO-	S CONC	CONG.	ر د د د د د د د

RAM DATA - MIXTURE 3

63.5 % CO 36.5 % CO2

RET TIMESSEC	99•0	0.63			0.40	9010	0.77	1,61	1.01	2,61	1.7.1	70.4	4.33	7 0			00101	17.80	4.4.10	54,90	39.00	30.00	33.00	70.80	00.0		127400	133,20	266.40	306.00	•	200	٠,
SAMPLE	0140	C1402	0417		2011		20+13	C140	C1402	C140	C1402	0140	0.417	100	21	20412		20 + 13	C140	C1402	C140	C140	20413	C140	20417		) 1	C1402	C140	C1402	C140	200	0 1 1
PoPSIG	09*0	0,60	0.40	0.40			000	0 50	0.50	0.10	0 10	0.05	0.05				•	00.0	0000	00.0	0.10	0.10	0 1 0	0.50	0.50	00.0		00.00	00.0	00.0	00.0	00.0	<b>&gt;</b>
PIPPSIG	3+10	3.10	2 • 10	200	0 4 4		00.	06.	1 • 30	0.75	0.75	0 45	0 45	0+35	0.35	0000			C1 • 0	0 15	2•90	2,90	2.90	1,70	1.70	0.95		200	0.55	0.55	0.30	0.30	•
PA. IN HG	30.035	9.03	200	_	_				-	-	_	_	_		_			•	_	_	•	•	30,141	•	•	•		•	•	•	•		
TC.DEG C	205.8	ַ ב	ຍັ	ž	9	9	9	2	2 4	ַנַ פַ	Ţ,	Š	š	ř	5	9	9	4	5	<u>.</u>	ņ	ģ	ů	ŝ	ě	ŝ	4		C 00 2	206.5	206,7	206.7	
TR, DEG C	2216	ŭ.	Ñ	Ñ	ĕ	m	_			-	Ξ,	Ξ.	<u>.</u>	_	~	_	_		•	• .	•	•	•	•	•	٠	•	•	•	•	٠	•	
TOTAL FLOW RATE, CC/SEC	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4		2007	3,2154	2,6534	2,6534	1,8363	1.8363	4 . 0.6.2	0000 T		52 tr 10	0.0423	10000	0.3041	0.1411	0.1411	0,0640	0.0640	- COOP	C02007	1 0 20 3	1000	20000	2050.0	0.2934	0.2954	100140	1000	1010	070000	0 • 0 6 2 6	
COLUMN	SHORT			SHUKI	SHORT	SHORT	SHORT	SHORT	SHORT	TACHS		- 6000	2020	LAURA	SHORT	SHORT	SHORT	SHORT	SHORT	200		9 0 0 0	9 0	9 0	9 c	ב ב ב	LONG	LONG	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		9 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	5 C C C C C C C C C C C C C C C C C C C	

RAM DATA - MIXTURE 4

0,4 % CO 99,6 % CO2

COLUMN	TOTAL FLOW RATE, CC/SEC	TR, DEG C	TC+DEG C	PA. IN HG	PIPPSIG	POPPSIG	SAMPLE	RET	TIMESSEC
SHORT	4,6948	50.0	03,	30,680		0.55	0.4.0		1.35
SHORT	4,6948	50.0	03	30,680		50.0	01417		66.0
SHORT	3,7951	21.0	. 70	30,680		04.0	200		7 C
SHORT	3,7951	21.0	90	30,680		04.0			
SHORT	3,7951	21.0	04.	30,680		0.40	20017		999
SHORT	2,6774	21.0	03.	30.679			2010		
SHORT	2,6774	21.0	203.9	30.679	1 • 70	0 0	110		1.1
SHORT	2,6774	21.0	33	30,679		0.30	0140		000
SHORT	2,6774	21.0	3,	30,679		0.30	20.41.0		2.80
SHORT	1,8045	20.8	40	30,683		0.50	1413		
SHORT	1.8045	20.8	4.	30,683		0.00	21412		
SHORT	1.8045	20.8	. 40	30.683		0.00	61402		1.26
SHORT	1,0613	21.0	204.0	30,680		0.10	100		1.97
SHORT	1,0613	21.0	4.	30.680		0.10	01402		1.74
SHORT	0,5387	6.02	. 40	30,682		0.05	010		3.64
SHORT	0.5587	5000	. 40	30.682		50.0	2140		
SHORT	0.5887	20.9	4.	30.682		0.05	51402		3,7A
SHORT	0.3151	21.0		30,676		0.05	2010		9.67
SHORT	0.3151	21.0	204.1	30.676		0.05	51402		8 22
LONG	0.5574	21.0	3.	30.700		0.05	C140		15.20
LONG	0.5574	21.0	3	30,700		0.05	01402		5.80
LONG	0.3161	21.0	š	30.719		0.05	0140	Ξ	00.00
LONG	0,3161	21.0	5	30,719		0.05	01402	. Ξ	9.00
LONG	0.1616	21.1	3.	30.692		00.00	C140	· ~	9.90
LONG	0.1616	2101	8	30,692		00.0	21402	~	000
LONG	0.0627	21.5	205.3	30,769		00.0	0140	100	9.20
LONG	0.0627	21.5	Š	30,769		00.0	01402	100	9.00

RAW DATA - MIXTURE 5

94,7 % CO 5,3 % CO2

TIME, SEC	www.www.wwo.wo.wo.wo.wo.wo.wo.wo.wo.wo.w	-
		5
RET		÷
SAMPLE		•
PO.PSIG		>
PIPSIG	00000000000000000000000000000000000000	,
PA. IN HG	300 a do de	
C.OEG C	00000000000000000000000000000000000000	
TR.DEG C	00000000000000000000000000000000000000	
TOTAL FLOW RATE,CC/SEC	5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5	
COLUMN	SHORT SHORT SHORT SHORT SHORT SHORT SHORT SHORT SHORT SHORT SHORT CLONG LONG LONG LONG LONG LONG LONG LONG	

RAM DATA - MIXTURE 6

100.0 x CO

RET TIME, SEC	00000000000000000000000000000000000000	
SAMPLE	C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400 C1400	
POPPSIG		
PI » PSI G	MHHHH 4000000000000000000000000000000000	
PA. IN HG	22299 2111 212 22 23 24 24 24 24 24 24 24 24 24 24 24 24 24	
TC+DEG C	00000000000000000000000000000000000000	
TR, DEG C	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	
TOTAL FLOH RATE, CC/SEC	00000000000000000000000000000000000000	
NHULOO	SHORE SHORE CLONG	

RAM DATA - MIXTURE 7

0.0 % CO

RET TIME, SEC	0.74	0 0 0		1.07	0.72	1901	1.50	2,15	1.75	5,30	4.40	00.0	06.9	6.2	4.6	8.3	4.6	2.0	2.0	88.2	5.6	6.4	7.6		9	200
SAMPLE	C140		21412	0140	C1402	C140	C1402	C140	C1402	C140	C1402	0140	c1402	C140	C1402	C140	C140	C1402	C140	C1402	C140	C1402	C140	61402	C140	C1402
POPSIG	0,55	0.37	0.37	0.05	0,25	0 5 20	0.20	0.10	0.10	0.05	0.05	00.0	00.0	00.0	00.0	0 10	0.10	0.10	010	0.10	00.0	00.0	00.0	00.0	00.0	00 • 0
PIPPSIG	2.85			``	~	-	-	`	~	4	4	~	~	Ñ	Š	~	~	~	Ñ	Ñ	5	ŏ	ñ	ŭ	Ň	N
PA. IN HG	30.600			ě	Š	•	3	3	š	ě	3	ě	3	3	•	5	5	5	ç	5.	ູ້	2.	5	5.0	5	້
TC.DEG C	203.9	03.	03	04.	04.	04	•	94	04.	03.	03.	94	204.0	04.	04.	03.	03.	33.	04.	204,0	3	3	3	2	3	203.8
TR,DEG C	72. 72. 48.	2	Š	2	ċ	ż	ŝ	å	Š	ċ	å	ċ	ċ	ż	å	Š	ż	å	ċ	22.8	å	Š	å	Š	ċ	ຂໍ
TOTAL FLOW RATE,CC/SEC	4.5872	3,2051	3,2051	2.6432	2,6432	1.6495	1.0495	1,0417	1,0417	0.5398	0.5398	0.2978	0.2978	0.1276	0,1276	1,0477	1.0477	1,0017	0,5556	0+2556	0.3066	0 3066	0.1308	0.1308	0,0535	0, 0535
COLUMN	SHORT	SHORT	SHORT	SHURT	SHORT	SHORY	SHORT	LONG	LONG	SNON	LONG	LONG	CONC	LONG	LONG	LONG	LONG	LONG								

RAW DATA - MIXTURE 1

6.5 X CU

93.5 X C02

CATALYST ACTIVITY CHECKS

RET TIME, SEC	1950 1950 1760 1710 1640 1640 1640
SAMPLE	C140 C140 C1402 C1403 C140
PO.PS16	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
PlyPSlu	11111 •••••• ••••• •••• ••• ••• ••• •••
PA. IN HG	30.341 30.341 30.341 30.361 30.375
CADEG C	204.0 204.0 204.0 203.5 203.0
TR, DEG C	222.00 223.00 22.00 22.00
101AL FLUM RATE, CC, SEC	0.6.4332 0.0.4332 0.0.3332 0.0.445 0.4456
N E E	CONG CONG CONG CONG CONG CONG CONG CONG

RAW DATA

CARBON DIOXIDE - HELIUM RINARY MIXTURES

LONG COLUMN

PEAK TIME, SEC	7035.00 573.00 1470.00 2808.00 6372.00
PO, PS16	
PIPSIG	0000000
PA. IN HG	30.162 20.050 29.814 29.770 30.003
TC+OEG C	2004.4 203.5 205.0 205.0 205.0
TR.DEG C	22 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
TOTAL FLOW RATE, CC/SEC	0.2667 0.2695 0.2580 0.2580 0.2540 0.2454
700 x	7.30 26.90 14.20 10.00 12.40
MIXTURE	8 6 6 1 1 1 0 0 B 1 1 1 1 1 1 1 1 1 1 1 1 1 1

RAM DATA

1988 VULUME OFFERMINATIONS

HELIUM CARRIER GAS = ARGON SAMPLE

COLUNA	TOTAL FLUIN RAFE, CC/SEC	TAMBES C	0.90000	pa. Iv HG	PINPSIG	Pr.PsIG	PFAK TIME, SEC	BYPASS FRACTION
LANG	0.4079	23.8	207.3	30,237	1.50	0.05	36,30	0.232
PAD.I	3.4079	23.8	207.3	30,237	1.50	50.0	36.20	0.230
L '1 V i	0.4374	23.d	207.3	30.237	1.50	0.05	36.20	0.226
£-1 V-3	0.4079	23.3	201.3	30.237	1.50	50.0	36.20	0.223
1,000	3.1473	23.9	207.1	30,230	0.40	00.0	71.40	0.228
( ) ( )	0.1975	< 3°3	207.7	30,230	0.40	00.0	72.00	0.231
6 V O T	0.1975	23,9	207.7	30,230	0.40	00.0	72.60	0.231
1000	0.1255	< 3° 7	207.4	30.226	0.55	00.0	111.00	0.228
LONG	0.1255	23.9	207.4	30,226	0.55	00.0	111,60	0.232
LOWG	0.1255	43.4	201.4	30.226	0.55	00.0	111.00	0.229
SHUAL	0.4402	23.9	2.11.4	30,227	0.15	00.0	2.89	
SHORT	0.2556	23.3	506.3	30,223	00.0	00.0	4.65	
SHURT	0.1238	43.1	206.7	30,227	00.0	00.0	9.41	

SHURL SUCURY PEAR 1146 JAILJES ARE AVERAUE VALUES

# APPENDIX H

# CALCULATED RESULTS

CALCULATED RESULTS - MIXTHRE 1

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1.1184 788.6
0.3151
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1403
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0.3811 A02
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0.0984

CALCULATED RESULTS - MIXTHRE 2

27.6 % CO 72.4 % CO2

The St C	COLUMA	FLON RATE, CC/SEC, CRLUMY CONDITIONS	PC. MM HG	SAMPLE	G* X 100000.
02.0	SHURT	6.34.R	Š	÷	
0.36	Sr.1 R.1		O • 0 1 0	2412	7.109
£ 1, 5	SHIPT	0 100 0	850.9	C1402	1.570
6.26	FRORS	•	824.4	C 1 4 U	7.725
6,33	SHORT	\$-C03-6-6-6-6-6-6-6-6-6-6-6-6-6-6-6-6-6-6-6	824.4	C1405	•
6.0	TAILES.	3 4 1 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	814.3	C140	•
ت ان ان	SHCB1	•	814.3	C1402	•
05.0	54001	•	0.667	C140	•
82.0	SHORI	200	199.0	C1402	•
0.78	SHIRT		7.96.2	C14P	•
1.12	TOURS		786.2	C1405	•
	CHOCH		778.5	C140	_
88.	SHIRT	162141	776.5	C1402	1.268
	Talla?	1,000,0	797.4	C140	_
2.54	10017	1598-0	797.4	C1402	
2.5	SHIPT	DE 64 - 6	773.6	C140	7.011
4.17	CB(10.1	## A # • O	773.6	C1412	1.829
4.17	1023	0.500	769.4	C140	6.718
6.87	TOURS	00840	769.4	C1405	
, E	Tages	1201-0	770.0	C140	
10.30	SHUBT	0.1421	770.0	C1405	3.151
10.30	100 H	112110	768.6	C14U	
14.70	430		768.6	C1405	
14.70	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	10000	845.3	C14N	
22.00	5 S S S S S S S S S S S S S S S S S S S	0.245.6	845.3	C1412	
22.00	SND	•	820.5	C140	
24.40	ت د د ا	000140	820.5	C1402	
44.80	2 × C	•	2.062	C14:0	
75.44	2001	•	793.3	C 1 4 D	
91.40	2 2 2	2.4.4.5.4.5.4.5.4.5.4.5.4.5.4.5.4.5.4.5.	793,3	C1412	
31.8	9 N I	•	782.3	C14D	
185.60		5 C C	782.3	C1413	6.513
185.80			773.3	-	7.215
) )		\0\n\0\n\0	773.3	C1413	41

CALCOLATED RESULTS - MIXTORE 3

63.5 x C0

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TR.SEC	CULUMA	FLUM RATESCUZECSCHEUMN COMBITIONS	PC.MM HG	SAMPLF	G* X 100000.
					;
70.0	SHURT	6.7344	858.6	C14n	3.279
	SHIRE	5.7380	856,6	C14U2	3.023
07.0	12057	4.605	828.6	C14:0	3.432
(	SHURT	4.6651	824.6	C1405	2 • 0 6 2
9 4 6	SHORT	3. BORR	818.5	C14U	2.274
1	A TIBLE	3.8988	818.5	C1413	1.380
- T		2.7493	803.2	C140	3.043
79.0	SACET	2.7403	803.2	C1402	\$ • 087
2 - 1	1 KO 7 K	1.5987	786.4	C14n	2.684
	18048	1.5947	7.96.4	C14U5	1.014
	5.40.81	9.8388	777.4	C 1 4 U	2.621
2.00	SHURE	J. B. B. B. B.	777.4	C1412	2.025
	340H2	3.4727	773.4	C110	2.681
3.0	(S) 0.5	10101	773.4	C14U2	2.033
7 7 7	SHURI	1)+2206	769.3	C140	2.546
3.44	54047	4.2204	769.3	C14112	2.847
: ::::::::::::::::::::::::::::::::::::	3 4URT	10100	761.9	C14n	2,912
08.81	SHUNT	4601.0	767.9	C1405	4.142
14.90	LUNG	1.1313	843.2	C141	2.715
14.4	LUNG	1.1313	843.2	C1405	2.140
26.80	LUNG	0.6299	911.1	C14U	2.656
2 4 4 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	CONC	0.55.99	811.1	01402	P.656
5.83	540J	0+3473	790.4	C140	2.627
4 11 5 0	57.5	Ex+E+0	790.4	C1402	P.743
04.70	5707	0.1179	779.8	C 14()	2.80%
	SUDI	0.1779	8.5/2	C1402	3.457
223.5	LCNG	3.0755	172.0	C140	6.633
223.80	ריגעט	0.0755	772.0	C1415	7.561

CALCULATED RESULTS - MIXTHRE 4

00 % 4.0

99.6 % CO2

TROSEC	CULUMN	FI.CK RAIE, CC/SEC, COI, UMN CONDITIONS	PC.MM HG	SAMPLE	G* X 100000.
0.28	SHORT	6.6710	868.5	C140	9.203
0.28	SHURI	0.6710	868.5	C1402	3.876
0.34	SHORT	5.4981	851.7	C140	6.676
0.34	SHURI	5.49A1	851.7	C140	10.490
0.34	SHORT	5.4981	851.7	01402	2.233
0.47	SHORT	3,9741	831.0	C140	2,213
0.47	SHUR1	3.9701	831.0	C140	3.144
0.47	Sn081	3.0711	831.0	C1402	2.213
0.47	SHORT	3,9741	A31.0	C1402	1.968
0.68	SHURT	2.7330	815.5	C 1 4 D	2.080
0.68	SHORT	2.7330	815.5	C1405	1.914
0.68	SHURI	2.7331	815.5	C1405	2.014
1.14	SHURT	1.6315	802.5	C140	1.165
1.14	S.40.8.1	1.6316	802.5	C1402	1.611
2.14	SHURT	0.8694	793.5	C140	1.534
7.14	SHOAT	1.0004	793.5	C1405	1.555
2.14	SHURT	0.869a	793.5	C1402	1.677
3.78	SAURT	0.4933	788.2	C14U	2.823
3.78	SHORT	0.4933	788.2	C14U2	2.364
26.10	£ 10.14 ii	0.6454	821.2	C14D	3.717
26.10	LUNG	0.6459	821.2	C1412	30.55.55
97.10	1.0%	0+1935	773.8	C140	5.060
87.10	ยพญา	0.1935	793.8	C1402	4.995
45.00	r 1) N G	3.3743	806.1	r.14n	4.391
45.00	L U 4 G	0.3743	806.1	C14U2	4.391
222.00	L.กง <u>ติ</u>	0.0751	786.7	C140	5.995
222.00	i. ONG	0.0741	786.7	C1402	6.114

CALCULATED RESULTS - MIXTURE 5

94.7 % CU

5.3 % 002

TR.SFC	COLUMN	FLOW KATE, CUZSEC. COLUHN CONDITIONS	PC.MW HG	SAMPLF	G* X 100000.
9	10013	1,000			****
100	10000		A = 7 × 0		
0.0	2000	TURCE	A - 1 - 2	7 T T T	0 1 1 1 1 1
0.39	SHURT	4.8034	834.4	C140	0.789
0.39	SHURT	4.8034	834.4	C1402	10.900
0.43	SHURI	4 • 1 3 0 3	824.0	C140	2.018
0.45	SHURT	4 • 1 3 0 5	824.0	C1405	19.680
0.75	SHURT	2.4943	801.8	C14n	1.551
0.75	SHURT	2.4943	801.8	C1412	11.900
1.28	SHURT	1.4512	790.3	C140	1.863
1.28	SHURT	1.4512	796.3	C1402	11.220
2.08	SHURT	0.9055	784.3	0140	1.752
5.06	SHURT	0.9055	784.3	C1405	10.750
2.06	SHORT	0.9055	784.3	C1402	11.130
4.15	SHORT	0.4478	713.2	C140	1.988
4 - 15	SHURT	0.4478	779.2	C1402	7.852
91.9	SHORI	0.2749	774.8	C14P	8.208
6.76	SHURT	0.2749	774.8	C1402	6.572
27.20	LONG	0.6198	814.3	C140	<b>8</b> 003
27.20	LUNG	0.6198	814.3	C1402	P . 398
49.10	L C ≥ G	0.3436	794.6	C140	1.945
49.10	FUNG	0.3436	794.6	C1405	2.372
103.90	LCNG	0.1627	780,5	C14C	2.015
103.90	LUNG	0 • 1627	780.5	C1402	2.376
191.30	L ( . lv G	0.0683	778.7	C141	2.217
191.30	LUNG	U•PBB3	178.7	C1402	2.462

CALCOLATED RESULTS - MIXTURE 6

100.0 % 0.001

200 % 0.0

TK, SE C	COLUMN	FLOW RATE, CL/SEC, COLUMN CONDITIONS	PC.MM HG	SAMPLE	G* X 100000.
97.0	SHBRI	4.0290	817.1	C140	1.991
94.0	· SHURT	0670 · h	817,1	C1403	53.770
0.55	Shurt	3.3999	808.2	C 1 4 J	1.469
0.55	SHURT	3.3929	808.2	C1402	21.530
26.0	SHURT	2.0396	790.0	2140	1.572
0.92	SHURT	2.030A	790.0	C1402	26.790
1.52	SHORT	1.2272	778.5	C14P	1.776
1.52	SHURI	1.8272	778.5	01402	11.800
96.2	SHORT	0.6276	774.6	C140	1.719
76.2	SHURI	0.6276	174.6	C1405	10.580
5.27	SHORT	0.3579	768.3	C 1 4 0	1.839
5.27	SHLRI	0.3529	768.3	C1402	7.141
11.90	SHLRT	0.1546	767.0	C140	1.996
11.90	SHIRT	0.1566	767.0	C1405	5,303
17.30	PICN6	0.9747	829.4	C140	1.961
17.30	LONG	0.9747	459.4	C1402	2.449
30.50	P C N C	0.5525	802.4	C140	2,207
30.50	PNGT	0.5525	802.4	C1405	2.364
32.20	LONG	0.5242	797.9	C140	1.884
50.05	1.046	0.3327	788.4	C140	1.928
50.60	LONG	0.3327	788.4	C1402	2.189
97.20	PNOT	J.1736	775.3	C140	1.952
97.20	PONC	0.1736	775.3	C1402	2.278
201.60	LCAG	0.0840	768.0	C140	1.973
201.00	LUNG	0.0040	768.0	C1402	2.271
346.00	9NOT	0.0487	767.5	0110	2.167
346.00	LUNG	0.0487	767.5	C14U5	2.620

CALCULATED RESULTS - MINTHRF 7

0.0 \* 0.0

100.0 % 002

18,550	CULDEN	FLOW RAIF, CL/SEC, COLUMN CONDITIONS	PC. MM HG	SAMPLF	G* X 100000.
62.0	SHORI	5.4683	865.2	C140	3.751
50.0	SHUHI	5.4643	865.2	01402	9.668
0.40	SHURI	4.6601	A38.5	1812	1.743
0.40	SHGRI	4.6601	838	61402	1.917
0.48	SHORI	3.8950	828.1	C140	
0.45	SHUFF	3.8450	928.1	61402	1 - 159
0.75	CHIPT	6.4811	811.6	C14C	2.567
0.75	しょつ・ハ	2.4811	811.6	01402	9.239
1.17	SICRI	1.5994	0.667	C14D	1.852
1.1/	5-1UR]	1.5924	0.662	C1405	1.098
2.63	SHGRT	G+8330	791.4	C140	2.998
2.63	SHORI	0.8330	791.4	01402	2.118
4.62	SHURI	0.4631	7.96.3	C14D	2.636
4.(2	SHURI	0.4631	786.3	C1405	1.557
9.34	SHURI	0.1992	783.8	0140	4.294
<b>7.</b> €	THORS	2661.0	783.8	C1413	3.531
14.60	Lüng	1.1594	849.3	0.140	E 40.00
14.60	LONG	1.1594	849.3	0140	4.538
14.60	LUNG	1.1594	849.3	51413	8.312
26.56	L.ONC	0.6381	817.9	C140	4.713
26.50	LCNG	1 4 6 9 4 1	817.9	C1402	3.823
46.50	LUNG	0 • 3599	801.5	C 1 4 D	5.089
46.90	LUNG	0+3599	801.5	C1402	4.432
108.40	L C N G	0.1557	789.2	0140	5.382
108.40	LùvG	0.1557	789.2	C1402	4.998
262.50	1046	0.0643	782,2	C140	5.989
262.50	LONG	0+0643	782.2	C1402	5.864

CALCULATED RESULTS - MIXTURE 1

03
<b>64</b>
ı,

93.5 % C02

CATALYST ACTIVITY CHECKS

g* x 100000•	854.5	5,635	4.926	4.770	4.708	4 • 109
SAMPLE	0140	C140	C1402	0140	C140	C1402
PC.MM HG	8.197	8.767	797,8	798.8	798.7	798.7
FLOM RATE, CC/SEC, COLUMN CONDITIONS	8068 • 0	804840	0 • 3908	0 • 3915	0 • 40 4 3	0.4043
NWO TOO .	9007	5 80 3	LUNG	LONG	507G	LONG

TRASEC

CALCULATED RESULTS

CARBON FIOXIDE - HELIUM BINARY MIXTURES

## LONG COLUMN

6* X 10000.	20.450 1.520 3.950 7.840 16.890
FLOW HATE, CC/SEC, COLUMN CONDITIONS	0,3128 0,3153 0,3016 0,3085 0,2678
% C05	28.0 14.0 10.0 7.0 4.2
RIXTURE	90 0147

CALCULATED RESULTS
FREE VOLUME DETERMINATIONS
HELIUM CARRIER GAS = ARGON SAMPLE

COLUMN FREE VOLUME,CC	11 11 11 11 11 11 11 11 11 11 11 11 11
FLUM RATE, CC/SEC, COLUMN CONDITIONS	00000000000000000000000000000000000000
COLUMN	L L L L L L L L L L L L L L L L L L L

## APPENDIX I

## FORTRAN PROGRAM FOR COLUMN SIMULATION

```
W.D.SMITH, COLUMN SIMULATION PROGRAM
     DIMENSION X(500), Y(500), XA(500), YB(500), XB(500), YC(500)
1000 READ(5,10) DT, EPS, XT, YT, N, M
 10 FORMAT(4F10.0,215)
    READ(5,11) XI,YI,IX,IY
  11 FORMAT(2F10.0,215)
     READ(5,12) EK1, EK2, EK3, EK4, AZ, BZ
  12 FORMAT(6F10.0)
     READ(5,13) RK1, RK2, RK3, RK4
  13 FORMAT(4F10.0)
     READ(5,14) TM1, TM2, TM3, TM4, TM5
  14 FORMAT(5F10.0)
     READ(5,17) CZ,EK5,RK5
  17 FORMAT(3F10.0)
     WRITE(6,15) XT,N,AZ,BZ,EK1,EK2,EK3,EK4,RK1,RK2,RK3,RK4
  15 FORMAT(39H1 W.D.SMITH, COLUMN SIMULATION PROGRAM//
    119H CO MOLE FRACTION =,F6.3,4H N =,I5,5H AZ =,F6.3,5H BZ =,F6.3/
    26H EK1 =,F8.4,6H EK2 =,F8.4,6H EK3 =,F8.4,6H RK4 =,F8.4/
    36H RK1 =,F8.4,6H RK2 =,F8.4,6H RK3 =,F8.4,6H RK4 =,F8.4)
     WRITE(6,18) CZ,EK5,RK5
  18 FORMAT(5H CZ =,F8.5,6H EK5 =,F8.5,6H RK5 =,F8.6)
     WRITE(6,16) XI,YI
  16 FORMAT(5HOXI =,F8.4,5H YI =,F8.4)
     DO 20 I=1,500
     X(I)=0.
     Y(I)=0.
     XA(I)=0.
     YB(I)=0.
     YC(I)=0.
  20 XB(I)=0.
     IXPRN=C
     MIN=M
     IZ=0
     MTM=0
     MFAC=1
     MUL=1
     TFAC=1.
     A=AZ/(1.+EK1*XT)
     B=BZ/(1.+EK2*XT+EK3*YT*(1.+EK4/(EK2*XT)))
     C=CZ/(1.+EK5*YT)
     ZB=EK3*YT*B*EK4/(EK2*XT)
     F1=EK1*A
     F2=EK2*B
     F3=EK3*B
     F4=EK4*8/ZB
     F5=EK5*C
      WRITE(6,25) F1,F2,F3,F4,A,B,ZB
  25 FORMAT(5H0F1 =,F8.4,4H F2=,F8.4,5H F3 =,F8.4,5H F4 =,F8.4/
```

```
14H A =, F8.4, 4H B =, F8.4, 5H ZB =, F8.4)
    WRITE(6,26) F5,C
 26 FORMAT(5H F5 =, F8.5, 4H C =, F8.5)
100 DELT=DT*TFAC
    RT1=RK1 + DELT + A
    RT2=RK2*DELT*B
    RT3=RK3*DELT*8
    RT4=RK4*DELT*B
    RT5=RK5*DELT*C
    T1=(2.-DELT)/(2.+DELT)
    T2=2./(2.+DELT)
    T3=DELT/(2.+DELT)
    MTM=MTM+MFAC
    TCNT=MTM
    TIME=TCNT*DT
    XF=0.
    YF=0.
    IF(MTM.GT.IX) GO TO 110
    XF=2.*XI
110 IF(MTM.GT.IY) GO TO 115
    YF=2.*YI
115 I=IZ
    IS=1Z+1
200 I=I+1
    X0=X(I)
    Y0=Y(I)
    XAO=XA(I)
    XBO=XB(I)
    YBO=YB(I)
    YCO=YC(I)
    R1=RT1*(XO-XAO/F1)
    R2=RT2*(X0-XB0/F2)
    R3=RT3*(Y0-Y80/F3)
    R4=RT4*(Y80-X80/F4)
    R5=RT5*(Y0-YCO/F5)
    XA(I)=XAO+R1
    XP(I)=XBO+R2+R4
    Y8(I)=Y80+R3-R4
    YC(I)=YCO+R5
    XN=X0*T1+XF*T3-T2*(R1+R2)
    YN=Y0*T1+YF*T3-T2*(R3+R5)
    XF=XN+XO
    YF=YN+YO
    X{I}=XN
    Y(I)=YN
    IF(I.GE.N) GO TO 300
    IF(XN.GT.EPS) GO TO 200
    XN=O.
```

```
IF(YN.GT.EPS) GO TO 200
    YN=0.
    IF(I.GT.IS) GO TO 210
    IZ = IS
    IF(IZ.GE.N) GO TO 501
    GO TO 200
210 IF(I.LT.MIN) GO TO 200
    MIN=I
300 IF(TIME.LT.(TM1-EPS)) GB TO 400
    MFAC=2
    TFAC=2.0
    IF(TIME.LT.(TM2-EPS)) GO TO 400
    MFAC=5
    TFAC=5.0
400 TMUL=MUL
    TPRN=TMUL*TM3-EPS
    XPRN=IXPRN
    IF(TIME.LT.(XPRN*TM5)) GO TO 410
    IXPRN=IXPRN+1
    WRITE(6,402) (X(1),I=1,60)
    WRITE(6,402) (Y(I), I=1,60)
    WRITE(6,402) (XA(I),I=1,60)
WRITE(6,402) (XB(I),I=1,60)
    WRITE(6,402) (YB(I), I=1,60)
    WRITE(6,402) (YC(1), I=1,60)
402 FORMAT(1H0/(1H ,10F10.6))
410 IF(TIME.LT.TPRN) GO TO 500
    MUL=MUL+1
    XL=X(N)
    YL=Y(N)
    XY=XL+YL
    WRITE(6,401) TIME, XL, YL, XY
401 FORMAT(8H TIME =,F6.2,6H XL =,F8.5,6H YL =,F8.5,7H XL+YL=,
  1F8.5)
500 IF(TIME.LT.TM4) GO TO 100
    READ(5,510) IEND
510 FORMAT(I2)
    IF(IEND.GT.0) GO TO 1000
501 CALL EXIT
    END
```

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